



College of Engineering and Technology
Department of Basic and Applied Sciences
PHYSICS I – Sheet

Suggested Problems

- 1 Vectors
- 2 Coulomb's Law and Electric Field
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- 3 Electric Flux and Gauss's Law
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- 4 Electric Potential Energy and Electric Potential
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- 5 Capacitance
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31.46, 31.53, 31.55

Additional Exercises

1 Vectors

Question 1.1. If a person moves from the origin to point A with $x = 4$, $y = 3$, $z = 5$:

- a) Write down the displacement vector in cartesian form.
- b) What is the unit vector in the direction of the displacement ?

Question 1.2. For the following vectors:

- Find the unit vector $\hat{\mathbf{A}}$ in cartesian form.
- Find the polar forms of the vectors.

a) $\vec{\mathbf{A}} = 3\hat{\mathbf{i}} - 5\hat{\mathbf{j}}$ [Ans: $\hat{\mathbf{A}} = 0.5145\hat{\mathbf{i}} - 0.8575\hat{\mathbf{j}}$, $\vec{\mathbf{A}} = 5.831$, $\angle - 59.04^\circ$]

- b) $\vec{A} = -7\hat{i} - 15\hat{j}$ [Ans: $\hat{A} = -0.423\hat{i} - 0.906\hat{j}$, $\vec{A} = 16.553$, $\angle -115.02^\circ$]
 c) $\vec{A} = -3\hat{i} + 4\hat{j}$ [Ans: $\hat{A} = -0.6\hat{i} + 0.8\hat{j}$, $\vec{A} = 5$, $\angle 126.87^\circ$]

Question 1.3. Find the cartesian forms of the following vectors:

- a) $\vec{A} = 5$, 30° [Ans: $\vec{A} = 4.33\hat{i} + 2.5\hat{j}$]
 b) $\vec{A} = 10$, 257° [Ans: $\vec{A} = -2.25\hat{i} - 9.74\hat{j}$]
 c) $\vec{A} = 34$, 55° with the y -axis in the fourth-quadrant [Ans: $\vec{A} = 27.85\hat{i} - 19.50\hat{j}$]
 d) $\vec{A} = 55$, 25° with the x -axis in the third-quadrant [Ans: $\vec{A} = -49.85\hat{i} - 23.24\hat{j}$]

Question 1.4. A person moves from point $A(-2, 1, 7)$ to point $B(4, -3, -5)$.

- a) Find the displacement vector in cartesian form. [Ans: $6\hat{i} - 4\hat{j} - 12\hat{k}$]
 b) What is the magnitude of the displacement vector ? [Ans: 14]
 c) Find the unit vector in the direction of the displacement. [Ans: $0.428\hat{i} - 0.286\hat{j} - 0.857\hat{k}$]

Question 1.5. For the following force vectors acting on a body:

$$\vec{F}_1 = 5\hat{i} - 10\hat{j} \text{ (N)} \quad \vec{F}_2 = -15\hat{i} + 5\hat{j} \text{ (N)} \quad \vec{F}_3 = 4, \angle 45^\circ \text{ (N)},$$

what is the resultant force vector. [Ans: $-7.17\hat{i} - 2.17\hat{j}$ (N)]

Question 1.6. The vectors \vec{A} and \vec{B} are given as:

$$\vec{A} = -3\hat{i} + 4\hat{j} \quad \vec{B} = 4\hat{i} - 3\hat{j}$$

- a) Find the magnitudes of both \vec{A} and \vec{B} . [Ans: $|\vec{A}| = 5, |\vec{B}| = 5$]
 b) Put the following vectors in polar forms:

$$\vec{C} = \vec{A} - 5\vec{B}$$

[Ans: 29.83, $\angle 140.44^\circ$]

$$\vec{D} = 2\vec{A} + \vec{B}$$

[Ans: 5.385, $\angle 111.8^\circ$]

Question 1.7. [Scalar Product] Find the angle between the following vectors:

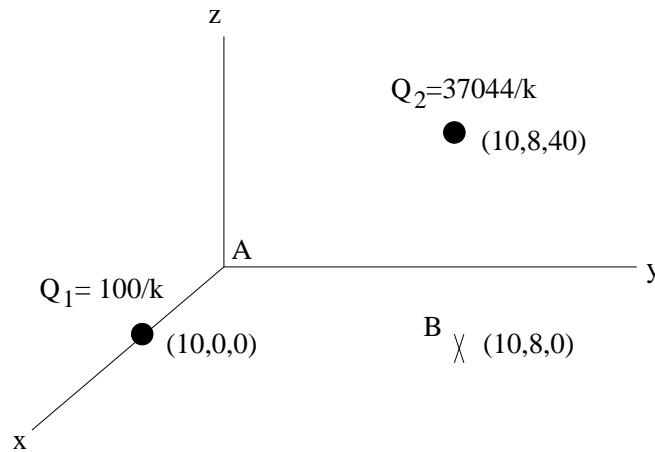
- a) $\vec{A} = 12\hat{i} - 15\hat{j} + 25\hat{k}$, $\vec{B} = -12\hat{i} + 20\hat{j} + 30\hat{k}$ [Ans: 75.201°]
 b) $\vec{A} = -10\hat{i} - 25\hat{j} - 50\hat{k}$, $\vec{B} = -12\hat{i} + 20\hat{j}$ [Ans: 106.67°]
 c) $\vec{A} = -10\hat{i} - 50\hat{k}$, $\vec{B} = -12\hat{i}$ [Ans: 78.69°]

2 Coulomb's Law and Electric Field

Question 2.1. Three charges, each of magnitude 3 nC , are at separate corners of a square of side 5 cm . The two charges at opposite corners are positive, and the other charge is negative. Find the magnitude of the force exerted by these charges on a fourth charge $q = 3\text{ nC}$ at the remaining corner. [Ans: $29.6\ \mu\text{N}$]

Question 2.2. A charge $Q_1 = \frac{100}{k}\text{ C}$ is located at $x = 10, y = 0, z = 0$. A charge $Q_2 = \frac{37044}{k}\text{ C}$ is located at $x = 10, y = 8, z = 40$. Let the coordinates of a point B be $x = 10, y = 8, z = 0$. Let A be the origin.

- Calculate the electric field vector at the point A : \vec{E}_A . [Ans: $\vec{E}_A = -6\hat{i} - 4\hat{j} - 20\hat{k}\text{ (N/C)}$]
- If a charge of $Q_3 = 2\text{ nC}$ is placed at the origin A , what is the electric force vector \vec{F} on Q_3 ? [Ans: $\vec{F}_{Q_3} = -12\hat{i} - 8\hat{j} - 40\hat{k}\text{ (nN)}$]

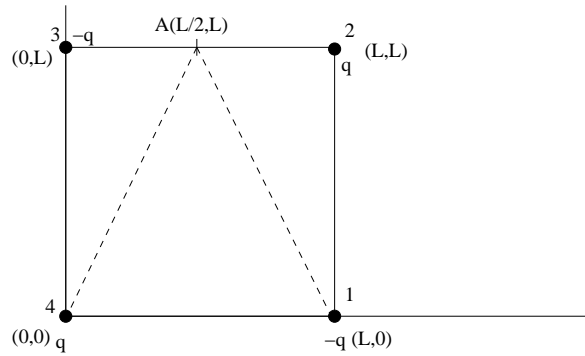


Question 2.3. A point charge of $5\ \mu\text{C}$ is located at $x = -3\text{ cm}$ and a second point charge of $-8\ \mu\text{C}$ is located at $x = 4\text{ cm}$. Where should a third charge of $6\ \mu\text{C}$ be placed so that the electric field at $x = 0$ is zero? [Ans: $(2.38\text{ cm}, 0)$]

Question 2.4. Four charges of equal magnitude are arranged at the corners of a square of side L as shown in the figure.

- Find the magnitude and direction of the force exerted on the charge in the lower left corner by the other charges. [Ans: $k\frac{q^2}{L^2}\left(1 - \frac{1}{2\sqrt{2}}\right)(\hat{i} + \hat{j})$]
- Show that the electric field at the midpoint of one of the sides of the square is directed along that side toward the negative charge and has a magnitude E given by:

$$E = k\frac{8q}{L^2}\left(1 - \frac{\sqrt{5}}{25}\right)$$



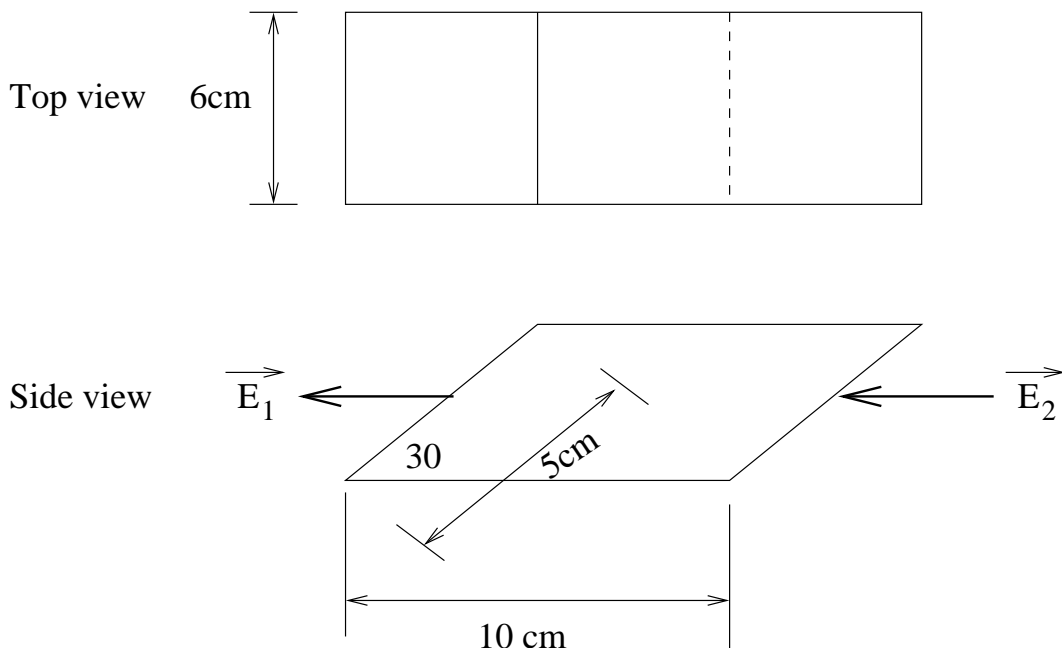
Question 2.5. A point charge of $-2.5\mu C$ is located at the origin. A second point charge of $6\mu C$ is at $x = 1\text{ m}$, $y = 0.5\text{ m}$.

- Find the x and y coordinates of the position where the electric field is zero. [Ans: $(-1.82\text{ m}, -0.91\text{ m})$]
- Find the x and y coordinates where the force on an: electron, proton, is zero. [Ans: $(-1.82\text{ m}, -0.91\text{ m})$]

3 Electric Flux and Gauss's Law

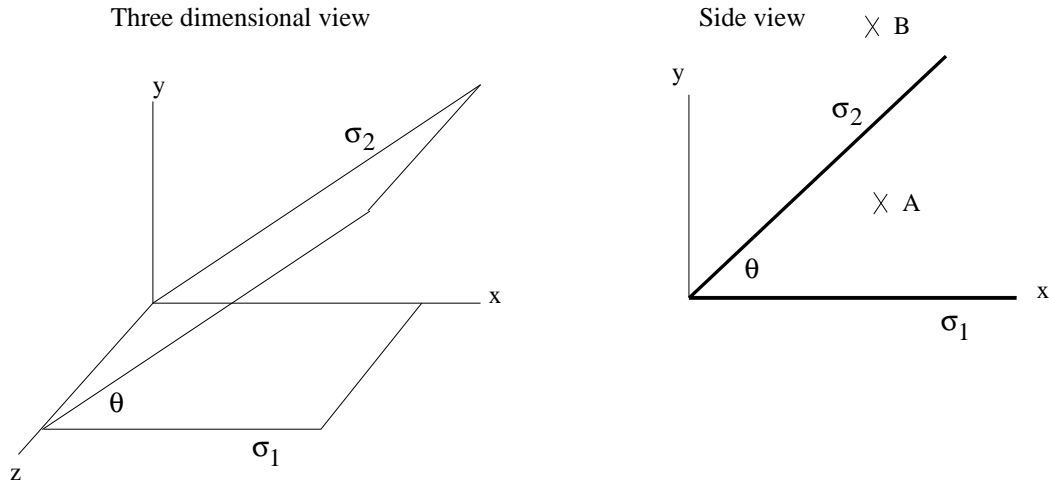
Question 3.1. Consider a uniform electric field $\vec{E} = 2\hat{i} - 3\hat{j} + 5\hat{k}$ (kN/C). What is the flux of this field through an area of 5 cm^2 with a normal vector of $7\hat{i} - 12\hat{j} + 17\hat{k}$? [Ans: $3.07 \times 10^{-3}\text{ N.m}^2/C$]

Question 3.2. A uniform electric field $\vec{E}_1 = -9 \times 10^4\text{ N/C}\hat{i}$, is directed out of one face of a parallelepiped, and another uniform electric field, $\vec{E}_2 = -11 \times 10^4\text{ N/C}\hat{i}$, is directed into the opposite face, as shown in the figure. Assuming that there are no other electric-field lines crossing the surfaces of the parallelepiped, determine the net charge contained within, and the average volume charge density. [Ans: $Q_{\text{inside}} = -0.2655\text{ nC}$, $\rho = -1.77\text{ }\mu C/m^3$]



Question 3.3. The electric field vector at the surface of the earth is 200 N/C toward the center. The field vector is reduced to 20 N/C at a height of 1400 m . What is the average volumetric charge density in the air enclosed between the earth surface and the height given ?
 [Ans: $1.13 \times 10^{-12} \text{ C/m}^3$]

Question 3.4. An infinite charged plane in the $z - x$ plane with a surface charge density of 70 nC/m^2 , a second infinite plane carrying a surface charge density of 50 nC/m^2 , intersects the $z - x$ plane at the z -axis and makes an angle of 40° with the $z - x$ plane as shown in the figure. Find the electric field at the point A ($x = 6 \text{ m}, y = 2 \text{ m}$), and the point B ($x = 6 \text{ m}, y = 8 \text{ m}$).



[Ans: $\vec{E}_A = 1815.7\hat{i} + 1790.8\hat{j} \text{ (N/C)}$, $\vec{E}_B = -1815.7\hat{i} + 6118.7\hat{j} \text{ (N/C)}$]

Question 3.5. An infinite plane of charge with surface charge density $\sigma_1 = 3\mu\text{C/m}^2$ is parallel to the xz plane at $y = -0.6 \text{ m}$. A second infinite plane of charge with surface charge density $\sigma_2 = -2\mu\text{C/m}^2$ is parallel to the yz plane at $x = 1 \text{ m}$. A sphere of radius 1 m with its center in the xy plane at the intersection of the two charged planes ($x = 1 \text{ m}, y = -0.6 \text{ m}$) has a surface charge density $\sigma_3 = -3\mu\text{C/m}^2$. Find the magnitude and direction of the electric field on the x axis at (a) $x = 0.4 \text{ m}$ and (b) $x = 2.5 \text{ m}$. [Ans: $\vec{E}_{x=0.4 \text{ m}} = 1.129 \times 10^5 \text{ (N/C)}\hat{i} + 1.695 \times 10^5 \text{ (N/C)}\hat{j}$, $\vec{E}_{x=2.5 \text{ m}} = -2.337 \times 10^5 \text{ (N/C)}\hat{i} + 1.212 \times 10^5 \text{ (N/C)}\hat{j}$]

Question 3.6. An infinitely long, thick, non-conducting cylindrical shell of inner radius a and outer radius b has a uniform charge density ρ . Find the electric field everywhere. [Ans:

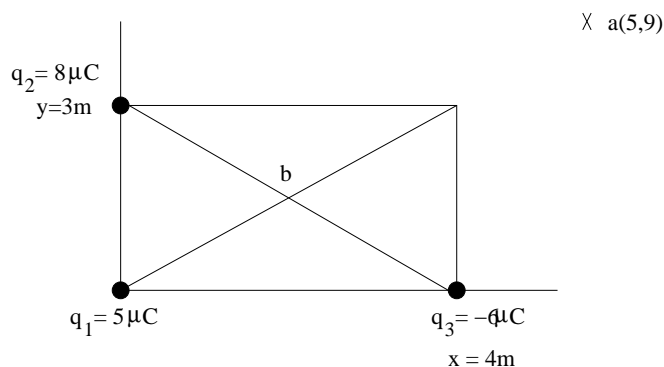
$$\vec{E}_{r \geq b} = \frac{\rho(b^2 - a^2)}{2\epsilon_0 r}, \quad \vec{E}_{a \leq r \leq b} = \frac{\rho(r^2 - a^2)}{2\epsilon_0 r}, \quad \vec{E}_{r \leq a} = 0]$$

4 Electric Potential Energy and Electric Potential

Question 4.1. Three point charges $5 \mu\text{C}$, $8 \mu\text{C}$, and $-6 \mu\text{C}$ are placed at the vertices of a rectangle as shown in the figure.

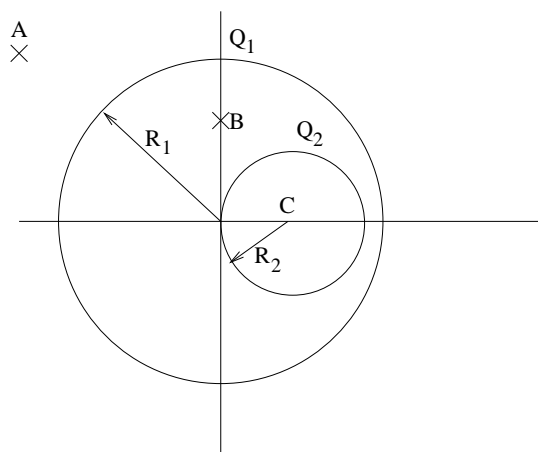
- Calculate the electric potential at points a with $x = 5 \text{ m}, y = 9 \text{ m}$ and b located at the center of the intersection of the diagonals of the rectangle. [Ans: $V_A = 7.6 \text{ kV}$, $V_B = 25.2 \text{ kV}$]
- What is the work done needed to move a charge of $4 \mu\text{C}$ from a to b ? [Ans: $W_{A \rightarrow B}^{\text{ex}} = 0.0704 \text{ J}$]

- c) What is the work needed to assemble the three charges q_1 , q_2 and q_3 ? [Ans: $U = -0.0339 J$]



Question 4.2. Two spherical shells of charge are as shown in the figure. Shell 1 has its center in the origin, with $R_1 = 5 m$, $Q_1 = 100/k$, and shell 2 has its center C at $x = 2 m$, with $R_2 = 2 m$, $Q_2 = 128\sqrt{2}/k$. Find:

- The electric field at point A with $x = -6 m$, $y = 8 m$. [Ans: $\vec{E}_A = -1.6\hat{i} + 1.8\hat{j} (N/C)$]
- The electric field at point B with $x = 0 m$, $y = 2 m$. [Ans: $\vec{E}_B = 16(-\hat{i} + \hat{j}) (N/C)$]
- The electric potential at point A . [Ans: $V_A = 26 V$]
- The electric potential at point B . [Ans: $V_B = 84 V$]
- The work needed to move a charge of $5 nC$ from A to B . [Ans: $290 nJ$]



Question 4.3. A spherical conductor of radius R_1 is charged to $20 kV$. When it is connected by a long, fine wire to a second conducting sphere far away, its potential drops to $12 kV$. What is the radius of the second sphere ? [Ans: $R_2 = \frac{2}{3}R_1$]

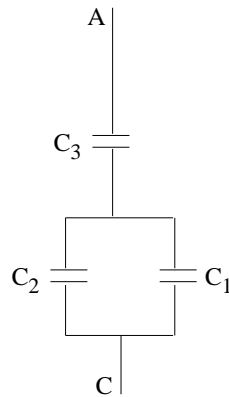
5 Capacitors

Question 5.1. A parallel-plate capacitor has square plates of size $10 cm$ and a separation of $d = 4 mm$. A dielectric slab of constant $\kappa = 2$ has the same area as the plates.

- a) What is the capacitance without the dielectric ? [Ans: 22.1 pF]
- b) What is the capacitance if the dielectric slab fills the space between the plates ? [Ans: 44.2 pF]
- c) What is the capacitance if a dielectric slab of thickness 3 mm is inserted into the 4 mm gap ? [Ans: 35.36 pF]

Question 5.2. In the following circuit of capacitors, where $C_1 = 3 \mu\text{F}$, $C_2 = 1.5 \mu\text{F}$ and $C_3 = 2 \mu\text{F}$:

- a) Find the equivalent capacitance between AC . [Ans: $1.3846 \mu\text{F}$]
- b) If a battery of 12 V is connected between A and C , find the total charge on the capacitors C_1 , C_2 and C_3 . [Ans: $Q_1 = 11.073 \mu\text{C}$, $Q_2 = 5.5365 \mu\text{C}$, $Q_3 = 16.61 \mu\text{C}$]



Question 5.3 (Final 2/1/2006).

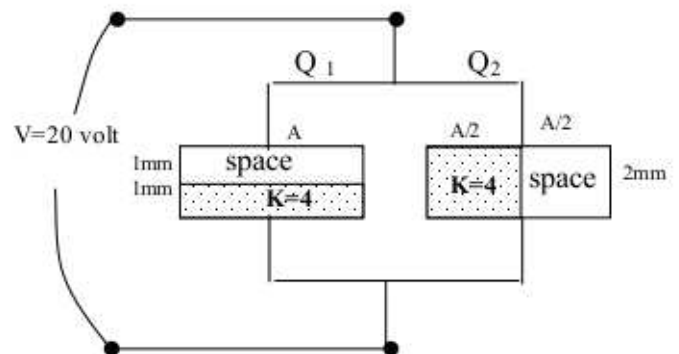
c) For the following capacitor circuit; find

• The equivalent capacitance

• The charges Q_1 and Q_2

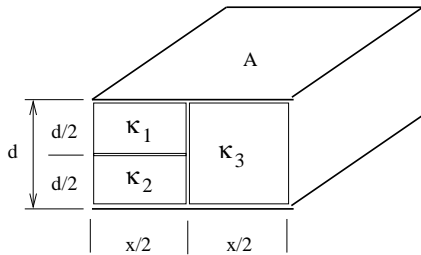
Consider the area of both capacitors

$$A = 1 \text{ cm}^2$$



1

Question 5.4. Find the capacitance of the parallel-plate capacitor shown in the figure.

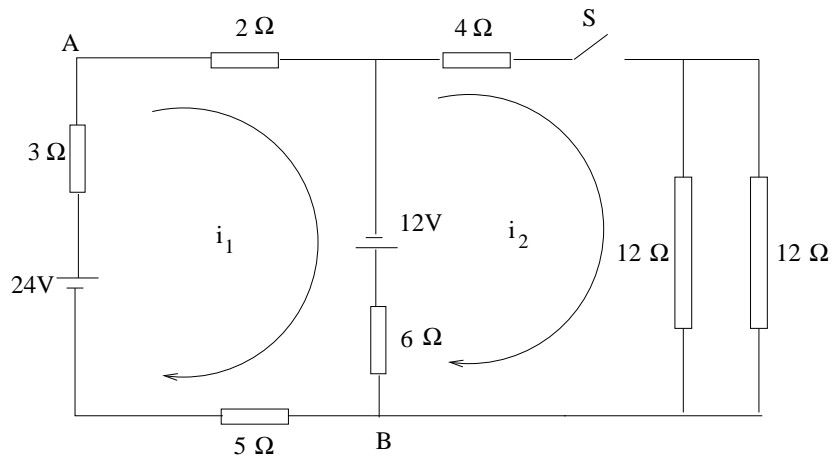


[Ans: $\left(\frac{\kappa_1 \kappa_2}{\kappa_1 + \kappa_2} + \frac{\kappa_3}{2}\right) C_0$]

6 EMF and DC Circuits

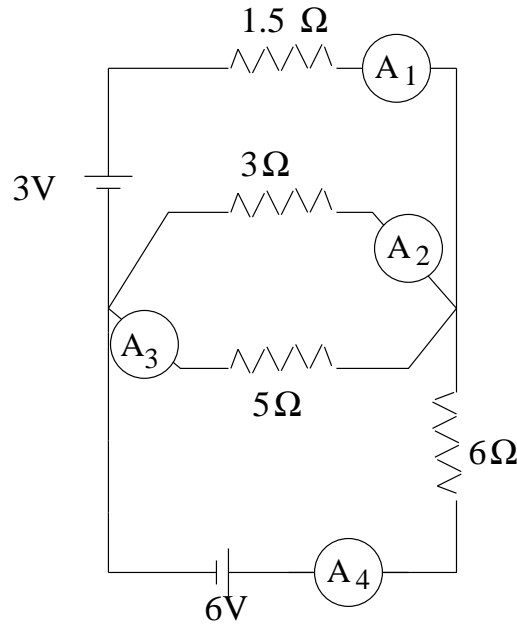
Question 6.1. In the circuit shown in the figure, find:

- The currents in the loops when S is open. [Ans: $2.25 A, 0 A$]
- The currents in the loops when S is closed. [Ans: $2.29 A, 0.109 A$]
(The questions below are to be answered when S is closed).
- The potential difference $V_{AB} = V_B - V_A$ between A and B . [Ans: $-5.7 V$]
- The power delivered by the $24 V$ emf. [Ans: $54.96 W$]
- The power dissipated in the 5Ω resistor. [Ans: $26.22 W$]



Question 6.2. In the circuit shown, find

- the readings of the ammeters,
- the power delivered by the $3 V$ emf,
- the power dissipated in the 6Ω resistor.



[Ans: $A_1 = 0.5365 A$, $A_2 = 0.7316 A$, $A_3 = 0.4390 A$, $A_4 = 0.6341 A$, $P_{3V} = 1.61 W$, $P_{6\Omega} = 2.413 W$]

7 Magnetic Force and Magnetic Torque

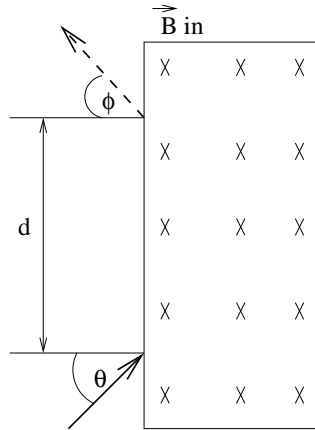
Question 7.1. Find the magnetic force \vec{F} on a charge $q = 5 \text{ nC}$ with velocity $\vec{v} = 3\hat{i} - 4\hat{j} + 7\hat{k} \text{ (m/s)}$, in a magnetic field $\vec{B} = 7\hat{i} - 10\hat{j} + 13\hat{k} \text{ (T)}$. [Ans: $\vec{F} = 90\hat{i} + 50\hat{j} - 10\hat{k} \text{ (nN)}$]

Question 7.2. A proton moving in a circular path perpendicular to a constant magnetic field takes $1.0 \mu\text{s}$ to complete one revolution. Determine the magnitude of the field. [Ans: $B = 0.06558 \text{ T}$]

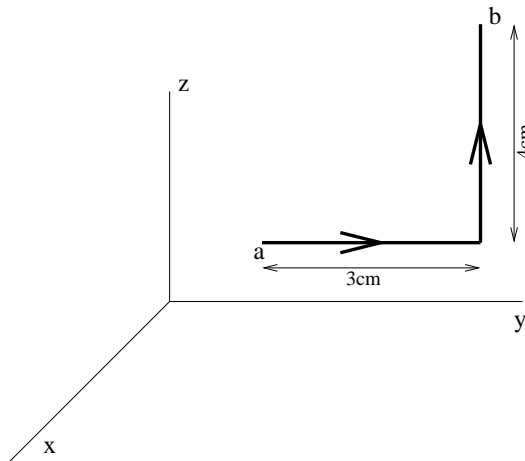
Question 7.3. A proton moves in a circular orbit of radius 65 cm perpendicular to a uniform magnetic field of magnitude 0.75 T .

- What is the period for this motion ?
- Find the speed of the proton.
- Find the kinetic energy of the proton.

Question 7.4 (Question 28.27, page 878). A proton with speed v enters a region of uniform magnetic field $B = 0.6 \text{ T}$, which is into the page as shown in the figure. Suppose that the distance $d = 0.4 \text{ cm}$ and $\theta = 24^\circ$. Find the speed v and the angle ϕ . [Ans: $v = 1.26 \times 10^5 \text{ m/s}$, $\phi = 24^\circ$]



Question 7.5. The wire segment in the figure carries a current of 1.8 A from a to b in the presence of a magnetic field of $\vec{B} = 1.2\hat{k}\text{ T}$. Find the total force on the wire. [Ans: $\vec{F} = 0.0648\hat{i}\text{ (N)}$]

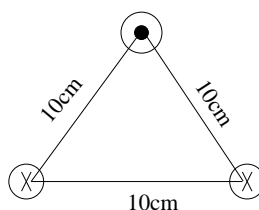


Question 7.6. A 10 cm length of wire carries a current of 2.0 A in the positive x -direction. The force on this wire due to the presence of a magnetic field B is $\vec{F} = 3\hat{j} + 2\hat{k}\text{ (N)}$. If this wire is now rotated so that the current flows in the positive y -direction, the force on the wire is $\vec{F} = -3\hat{i} - 2\hat{k}\text{ (N)}$. Determine the magnetic field vector \vec{B} .

8 Magnetic Field from an Electric Current

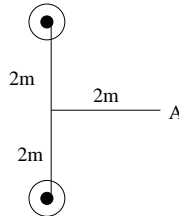
Question 8.1. Three long, parallel, straight wires pass through the corners of an equilateral triangle of sides 10 cm as shown in the figure. If each current is 15 A , find:

- The force per unit length on the upper wire. [Ans: $\vec{F} = 780\hat{j}\text{ (}\mu\text{N)}$]
- The magnetic field B at the upper wire due to the two lower wires. [Ans: $\vec{B} = 52\hat{i}\text{ (}\mu\text{T)}$]



Question 8.2. Two long parallel conductors each carry a 2 A current. The figure shows an end-view of the conductors, with both currents coming out of the page.

- What is the force per unit length acting on the two wires? Is it attractive or repulsive?
- Determine the magnitude and direction of the magnetic field at point B .



Question 8.3. A solenoid 2.7 m long has a radius of 0.85 cm and 600 turns. It carries a current I of 2.5 A . What is the approximate magnetic field B on the axis of the solenoid? [Ans: 0.7 mT]

Question 8.4 (Ampère's Law). A wire of radius 0.5 cm carries a current of 100 A that is uniformly distributed over its cross-sectional area. Find B

- 0.1 cm from the center of the wire. [Ans: 0.8 mT]
- at the surface of the wire. [Ans: 4 mT]
- at a point outside the wire 0.2 cm from the surface of the wire. [Ans: 2.86 mT]

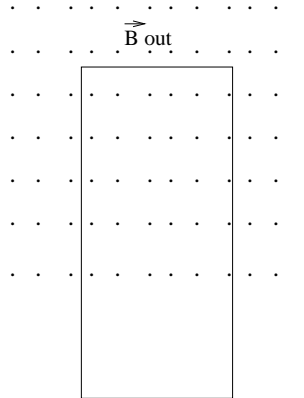
Question 8.5 (Ampère's Law). A tightly wound toroid of inner radius 1 cm and outer radius 2 cm has 1000 turns of wire and carries a current of 1.5 A .

- What is the magnetic field at a distance of 1.1 cm from the center? [Ans: 0.027 T]
- What is the field 1.5 cm from the center? [Ans: 0.02 T]

9 Magnetic Induction (Faraday's Law)

Question 9.1. A magnetic field $\vec{B} = 3t\hat{i} - 5\sin(5\pi t)\hat{j} + 17t^3\hat{k}$ (T) is applied at a coil with area $A = 3\text{ m}^2$, and with a normal vector $\vec{n} = 4\hat{i} + 5\hat{j} - 7\hat{k}$. Find the induced emf at $t = 4\text{ s}$. [Ans: $\mathcal{E}_{\text{ind}} = -1.925\text{ kV}$]

Question 9.2. The rectangular coil in the figure has 80 turns, is 25 cm wide and 30 cm long, and is located in a magnetic field $B = 1.4\text{ T}$ directed out of the page as shown, with only half of the coil in the region of the magnetic field. The resistance of the coil is 24Ω . Find the magnitude and direction of the induced current if the coil is moved with a speed of 2 m/s (a) to the right, (b) up, (c) to the left, and (d) down. [Ans: right 0 A , up 2.33 A (clockwise), left 0 A , down 2.33 A (counter-clockwise)]

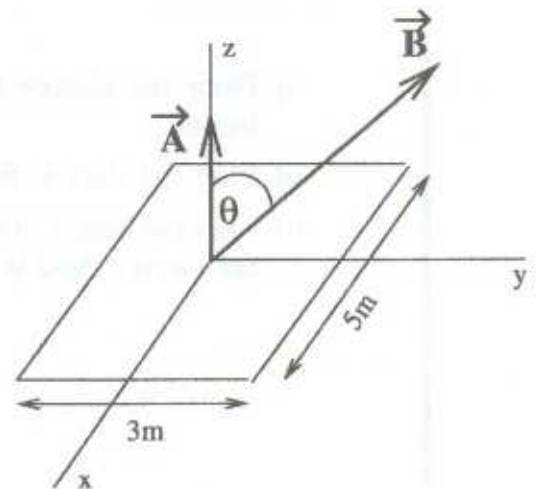


Question 9.3. Suppose the coil in Question 9.2 is rotated about its vertical centerline at constant angular velocity of 2 rad/s . Find the induced current as a function of time. [Ans: $I(t) = 0.35 \sin(2t)$]

Question 9.4. [Final 13/6/2004]

b) A rectangular coil with sides 5 m and 3 m , containing 200 turns lies on the xy -plane. A uniform magnetic field makes an angle of $\theta = 60^\circ$ with the positive z -axis, and its magnitude changes with time according to: $B(t) = 0.05t + 0.03t^3$.

- i) Find the magnitude of the induced emf in the coil at $t = 2 \text{ s}$.
- ii) Find the current in the coil if the resistance of the coil is 30Ω .
- iii) Find the torque acting on the coil at $\theta = 60^\circ$ and $t = 2 \text{ s}$.



A Constants

Coulomb constant	k	$9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$
Fundamental charge	e	$1.6 \times 10^{-19} \text{ C}$
Mass of electron	m_e	$9.11 \times 10^{-31} \text{ Kg}$
Mass of proton	m_p	$1.67 \times 10^{-27} \text{ Kg}$
Permittivity of free space	ϵ_0	$8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$
Permeability of free space	μ_0	$4\pi \times 10^{-7} \text{ N/A}^2$

B Theory

- Electric field due to an infinite plane of charge.
- Electric field due to a spherical shell of charge.

- Electric field due to an infinite line of charge.
- Electrostatic potential energy of a charge configuration.
- Capacitance of a parallel plate capacitor.
- Microscopic model of current: $I = nqvA$ (p.773).
- Circular motion of a charge in a magnetic field.
- Motional emf.
- Comparison between electric force and magnetic force.
- Units of all quantities studied in the course.
- All equations studied in the course.