

# EC332 Devices 2

Lecture 5

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# MOSFET as an amplifier

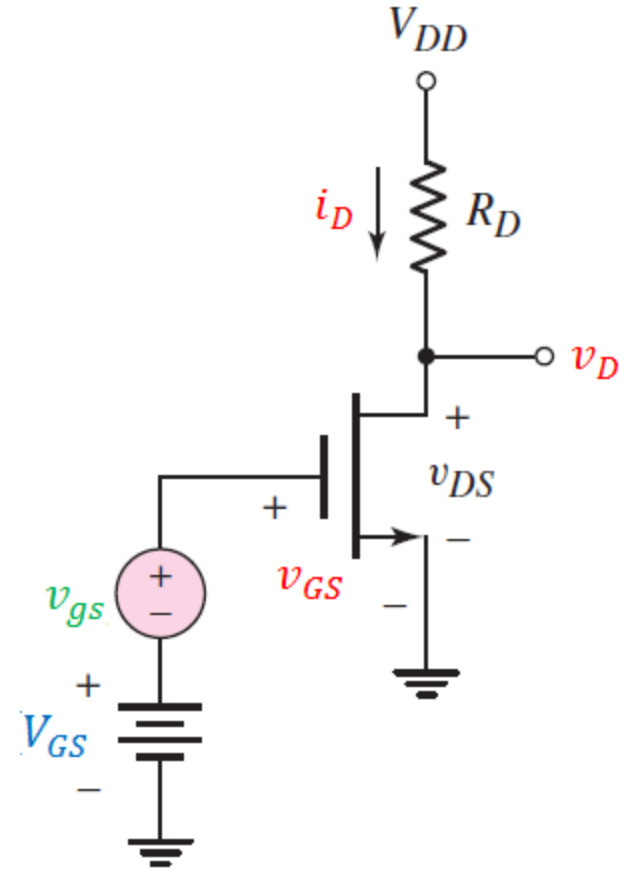
## Transconductance ( $g_m$ )

$$i_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (v_{GS} - V_t)^2$$

$$i_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( (V_{GS} + v_{gs}) - V_t \right)^2$$

$$i_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( (V_{GS} - V_t) + v_{gs} \right)^2$$

$$i_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( (V_{GS} - V_t)^2 + 2v_{gs}(V_{GS} - V_t) + v_{gs}^2 \right)$$



# MOSFET as an amplifier

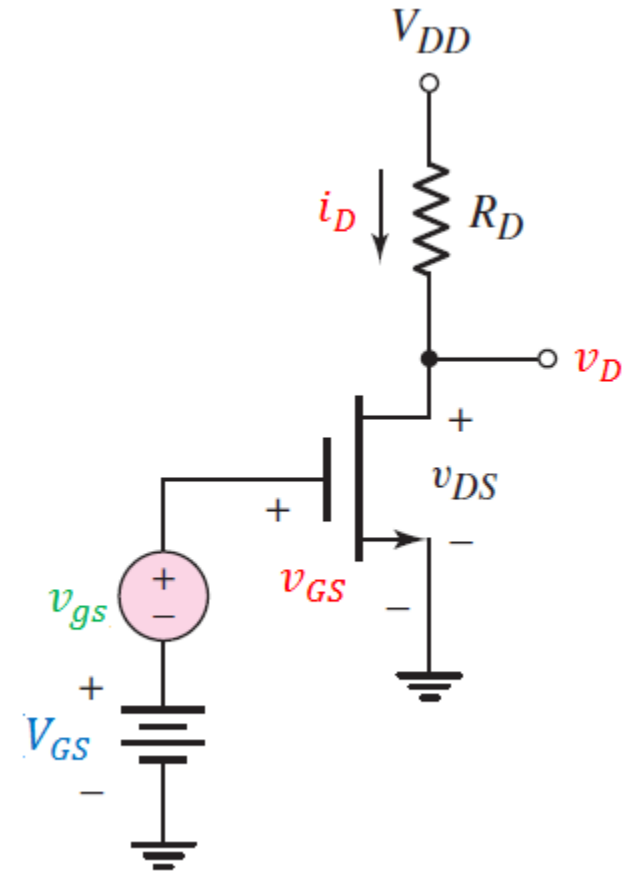
## Transconductance ( $g_m$ )

$$i_d = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( 2v_{gs} (V_{GS} - V_t) + \cancel{v_{gs}^2} \right)$$

Neglected  
for small signal i/p

$$i_d = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( 2v_{gs} (V_{GS} - V_t) \right)$$

$$i_d = \mu_n C_{ox} \frac{W}{L} v_{gs} (V_{GS} - V_t)$$



# MOSFET as an amplifier

## Transconductance ( $g_m$ )

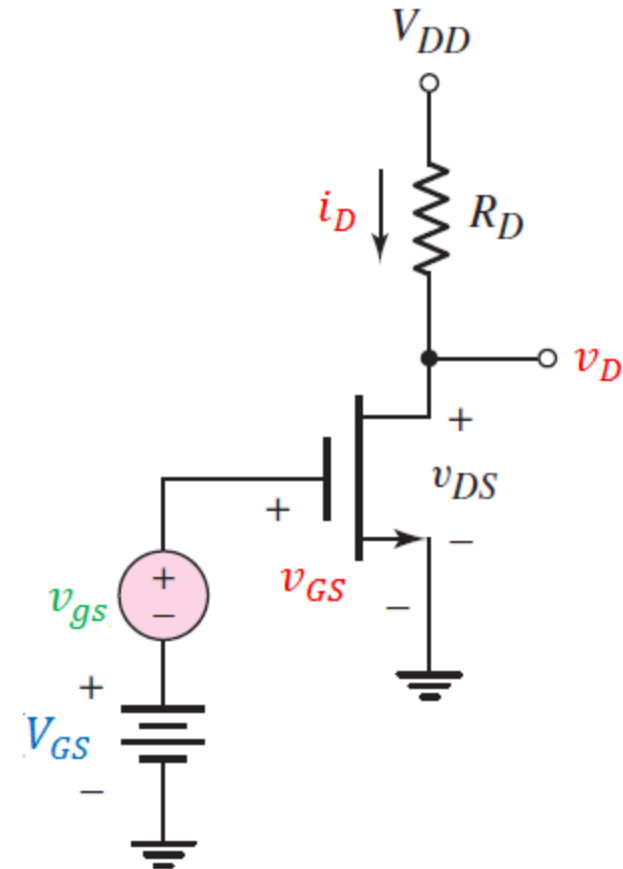
$$i_d = \mu_n C_{ox} \frac{W}{L} v_{gs} (V_{GS} - V_t)$$

$$\text{Define transconductance} = g_m = \frac{i_d}{v_{gs}}$$

$$g_m = \frac{i_d}{v_{gs}} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t)$$

$$\text{Recall: } I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t)^2$$

$$g_m = \mu_n C_{ox} \frac{W}{L} \sqrt{\frac{2I_D}{\mu_n C_{ox} \frac{W}{L}}} = \sqrt{2I_D \mu_n C_{ox} \frac{W}{L}}$$

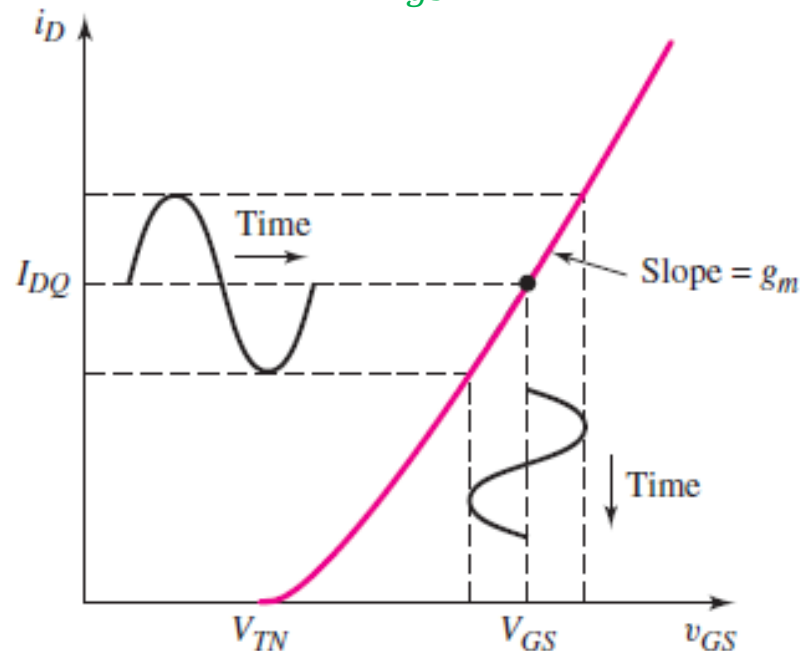


# MOSFET as an amplifier

## Transconductance ( $g_m$ )

$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t) = \frac{2I_D}{(V_{GS} - V_t)} = \sqrt{2I_D \mu_n C_{ox} \frac{W}{L}}$$

$$g_m = \frac{i_d}{v_{gs}}$$



# MOSFET as an amplifier

## Voltage Gain ( $A_V$ )

$$v_O = v_D = \underbrace{V_{DD} - I_D R_D}_{\text{DC}} - i_d R_D$$

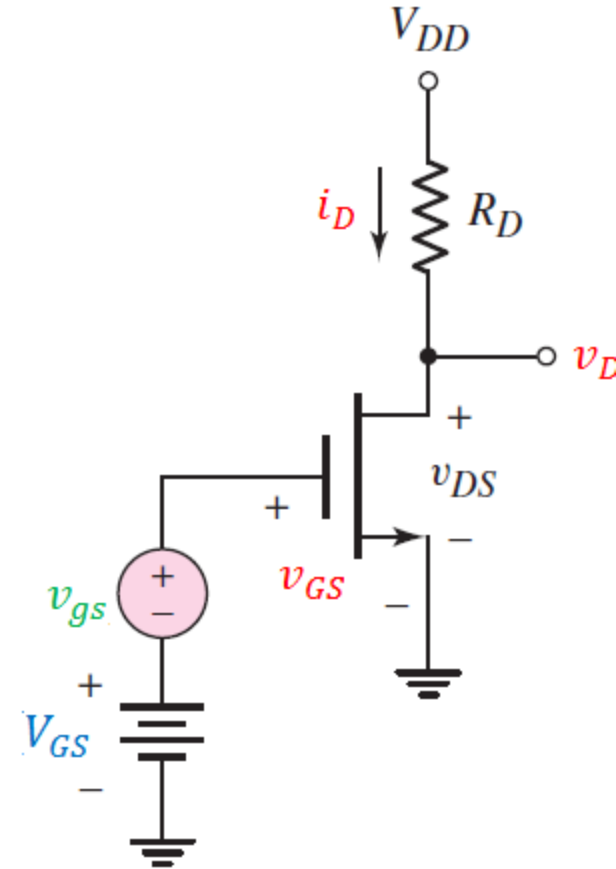
$$v_O = v_D = \underbrace{V_D}_{\text{DC}} - \underbrace{v_d}_{\text{AC}}$$

$$v_d = -i_d R_D$$

$$v_d = -\mu_n C_{ox} \frac{W}{L} v_{gs} (V_{GS} - V_t) R_D$$

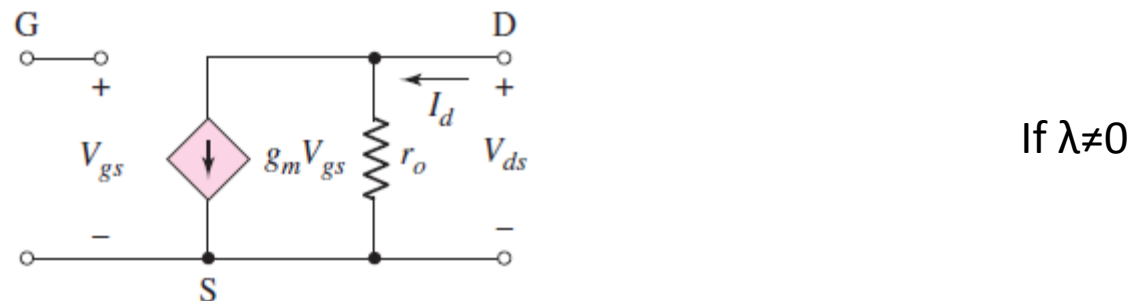
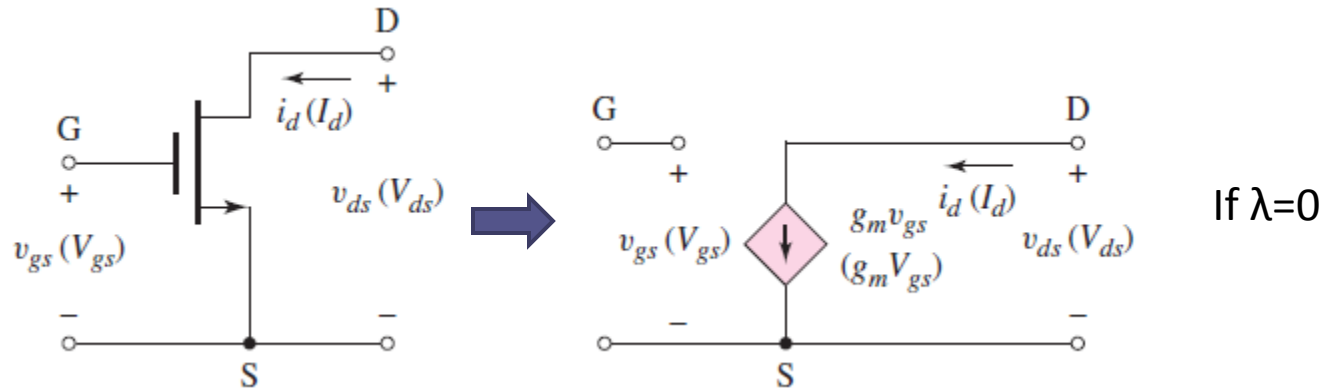
$$A_V = \frac{v_d}{v_{gs}} = -\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t) R_D$$

$$A_V = -g_m R_D$$



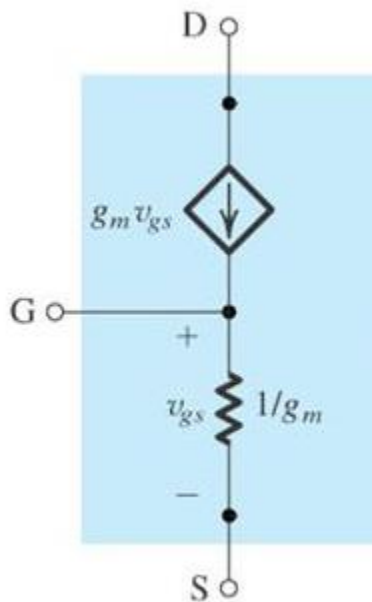
# Small Signal Equivalent Circuit Model

## $\Pi$ -Model

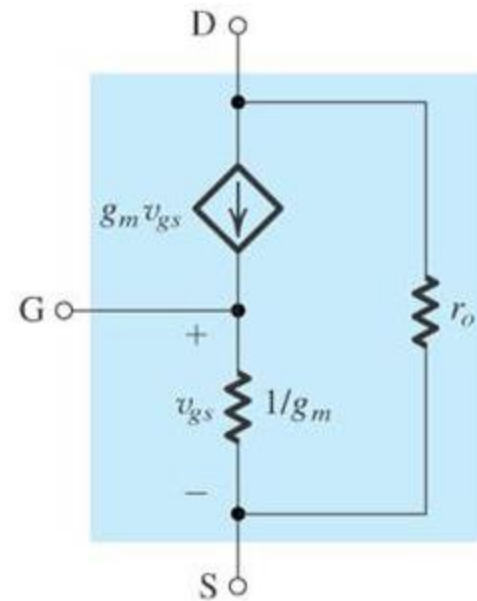


# Small Signal Equivalent Circuit Model

## T-Model



If  $\lambda = 0$



If  $\lambda \neq 0$