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MOS Capacitor

Lecture 6

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Advanced Devices (EC760)

Arab Academy for Science and Technology - Cairo

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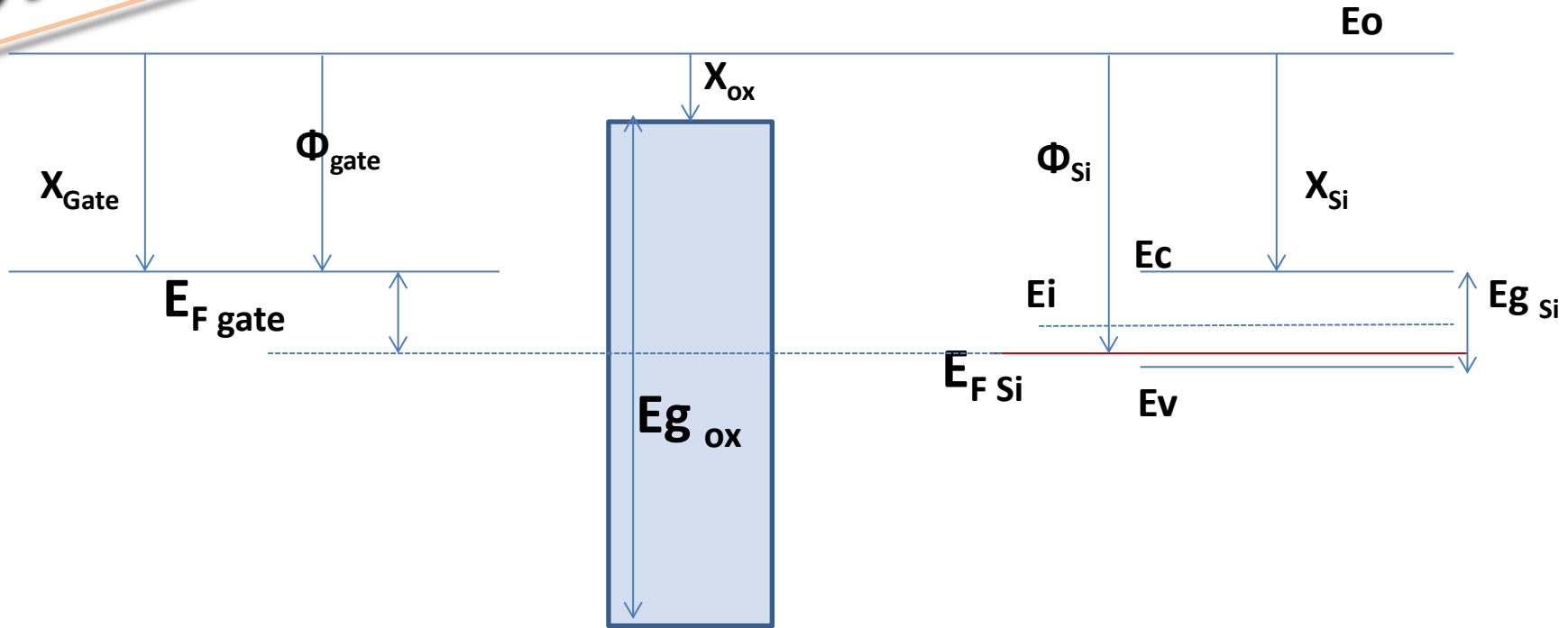
Outline



- Depletion Approximation
- Potential Drop Equation
- Threshold Voltage (V_{th}) and Flatband Voltage (V_{FB})
- Capacitance Voltage (C-V) Characteristics

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Flatband Voltage (V_{FB})

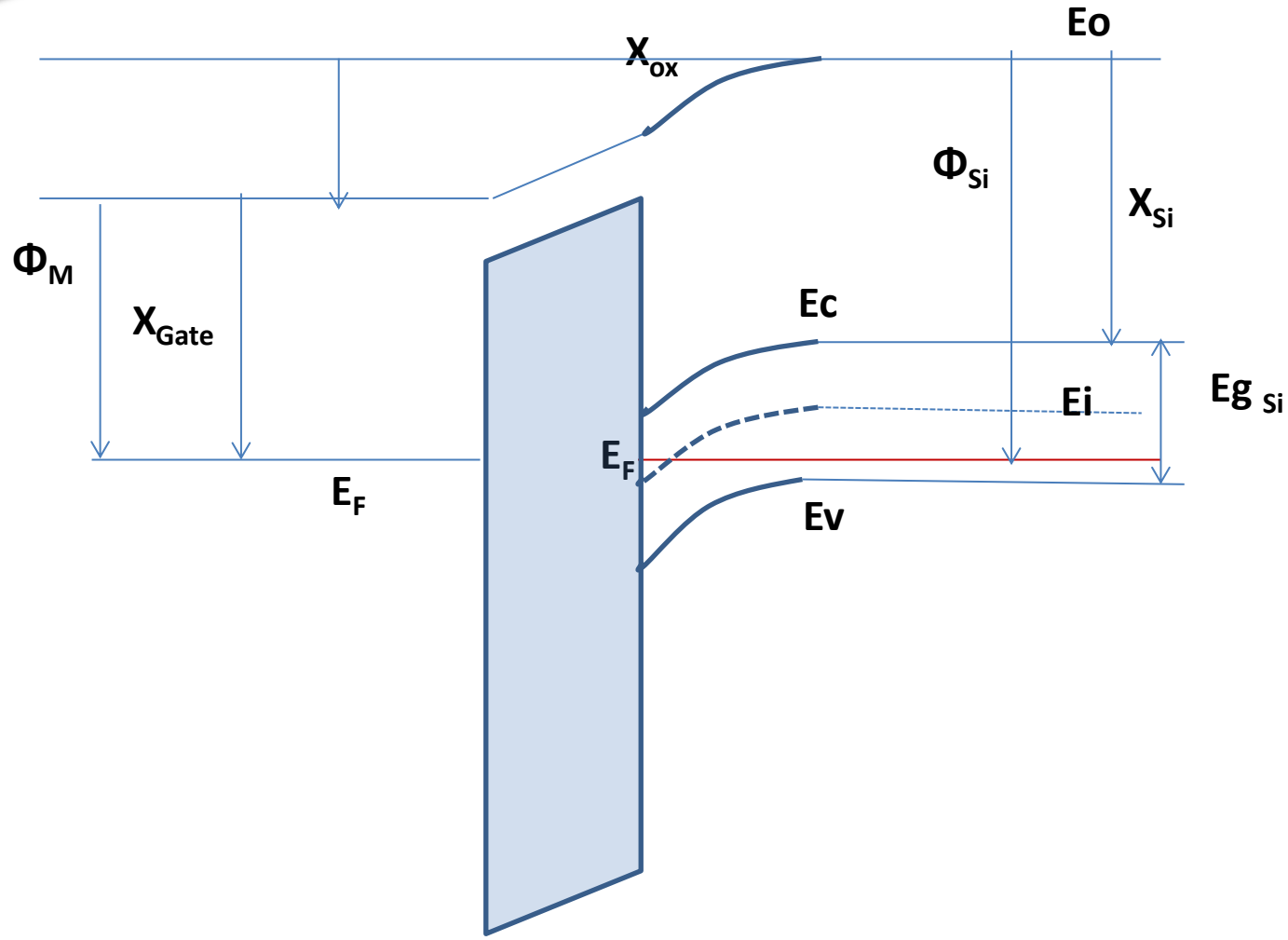


$V_{FB} = \text{Gate Workfunction} - \text{Semiconductor Workfunction}$

$$\begin{aligned} qV_{FB} &= \Phi_{gate} - \Phi_{Si} = E_{Fgate} - E_{FSi} \\ &= (X_{gate} + E_{Cgate} - E_{Fgate}) - (X_{Si} + E_{CSi} - E_{FSi}) \\ &= (X_{gate} + E_{Cgate} - E_{Fgate}) - (X_{Si} + K_B T \ln \frac{N_C}{N_A}) \end{aligned}$$

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Potential Drop Equation: No Applied Gate Voltage





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Potential Drop Equation: Applied Gate Voltage

$$V_g + (\Phi_{si} - \Phi_g) = V_{ox} + \Psi_s$$

$$V_g - V_{FB} = V_{ox} + \Psi_s$$

$$V_{ox} = -\frac{Q_s}{C_{ox}}$$

In Inversion:

$$Q_s = Q_{dep} + Q_{inv}$$

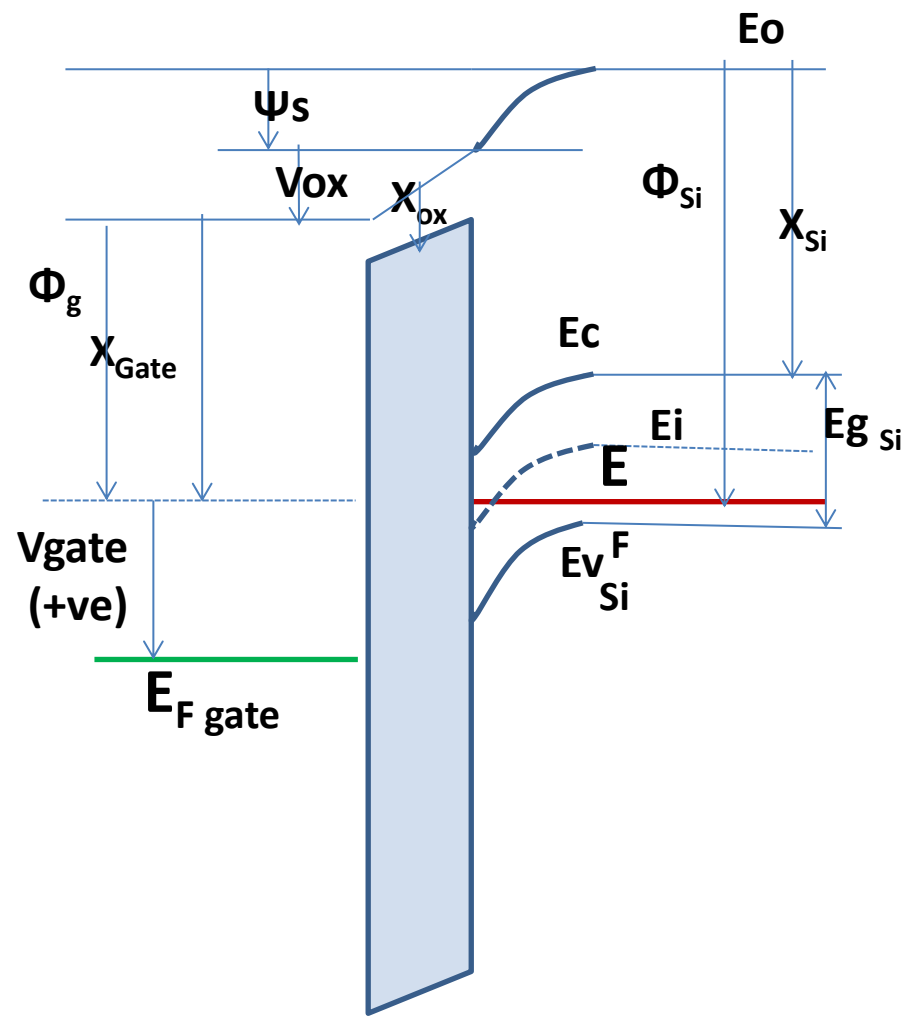
$$Q_{dep} = -qN_A W_{dep} = -\sqrt{2\epsilon_{si}qN_A\Psi_s}$$

In Strong Inversion:

$$Q_{inv} \approx -\sqrt{\frac{2\epsilon_{si}K_B T n_i^2}{N_A}} e^{q\Psi_s/2K_B T}$$

In-between: use Q_s equation

In Depletion: $Q_s \approx Q_{dep}$





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Threshold Voltage (V_{th}) under Depletion Approximation

At $0 > \Psi_s \geq 2 \Psi_{Bulk}$:

- No free carriers (i.e. no inversion electrons)
- Only depletion charges from ionized dopants

At $\Psi_s \geq 2 \Psi_{Bulk}$:

- No more changes in surface potential
- Fixed Q_{dep}
- Only changes in inversion electrons
- V_{gate} at $\Psi_s \geq 2 \Psi_{Bulk}$ is called Threshold Voltage (V_{th})

Using: $V_{gate} = V_{FB} - \frac{Q_s}{C_{ox}} + \Psi_s$

At “Onset” of Strong Inversion: $V_{th} = V_{FB} - \frac{Q_{dep}}{C_{ox}} + 2\Psi_{Bulk}$

$$= V_{FB} + \frac{\sqrt{2\varepsilon_{si}qN_A(2\Psi_{Bulk})}}{C_{ox}} + 2\Psi_{Bulk}$$



Inversion Charge (V_{th}) under Depletion Approximation (



In Strong Inversion ($V_g > V_{th}$):

$$V_{gate} = V_{FB} - \frac{Q_{dep} + Q_{inv}}{C_{ox}} + 2\Psi_{Bulk} = V_{FB} - \frac{Q_{dep}}{C_{ox}} + 2\Psi_{Bulk} - \frac{Q_{inv}}{C_{ox}}$$

$$V_{gate} = V_{th} - \frac{Q_{inv}}{C_{ox}}$$

$$\rightarrow Q_{inv} = -C_{ox}(V_{gate} - V_{th})$$

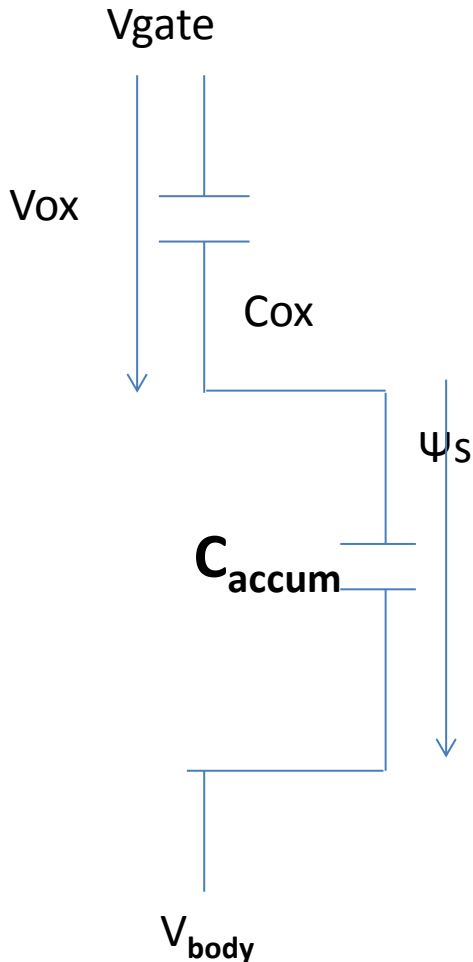


Capacitance-Voltage (C-V) Characteristics

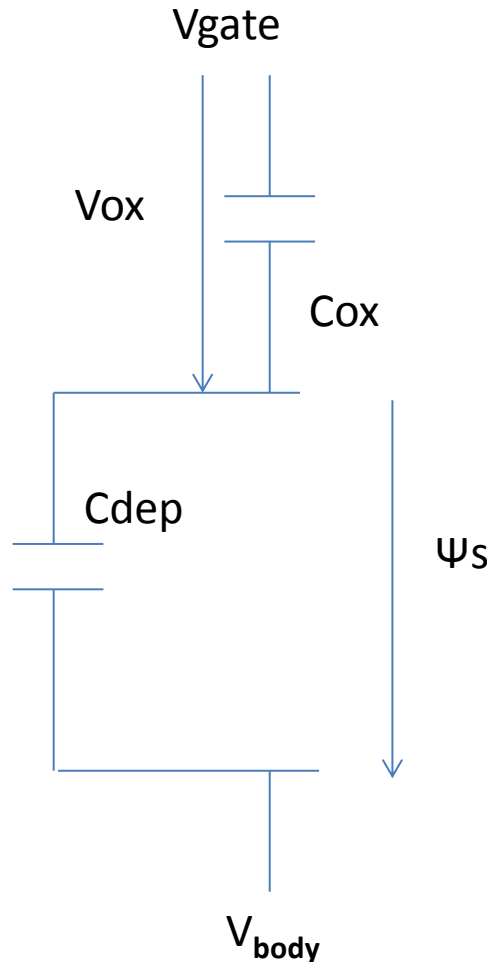
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$$\text{Small Signal: } C_C(V_g) = dQ_C/dV_C$$

Accumulation



Depletion



Inversion

