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MOS Stack

Lecture 4-5

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Outline

- MOS Band Diagram
- “Classical” Charge Distribution
- Depletion Approximation
- Potential Drop Equation
- Threshold Voltage (V_{th}) and Flatband Voltage (V_{FB})
- Capacitance Voltage (C-V) Characteristics





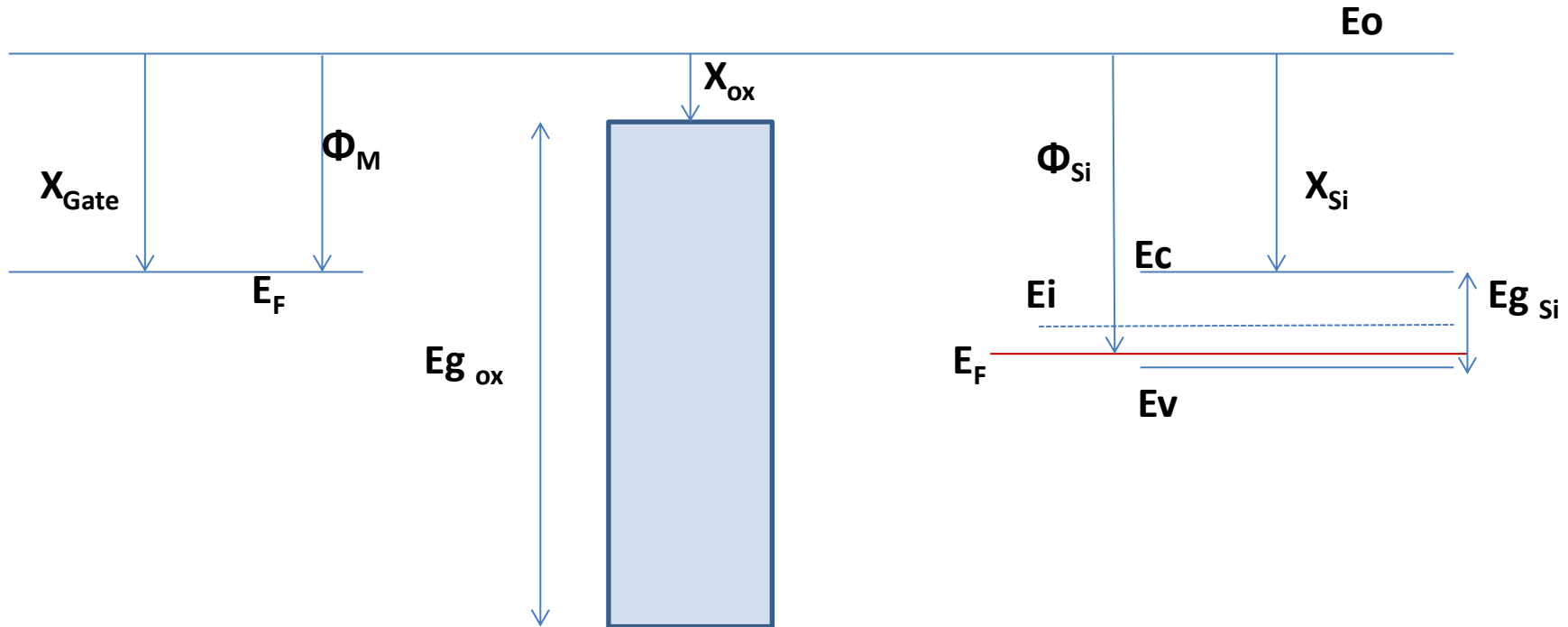
Reference

- Fundamentals of Modern VLSI Devices, 2nd Edition
by Yuan Taur , Tak H. Ning, Cambridge Press, 2013



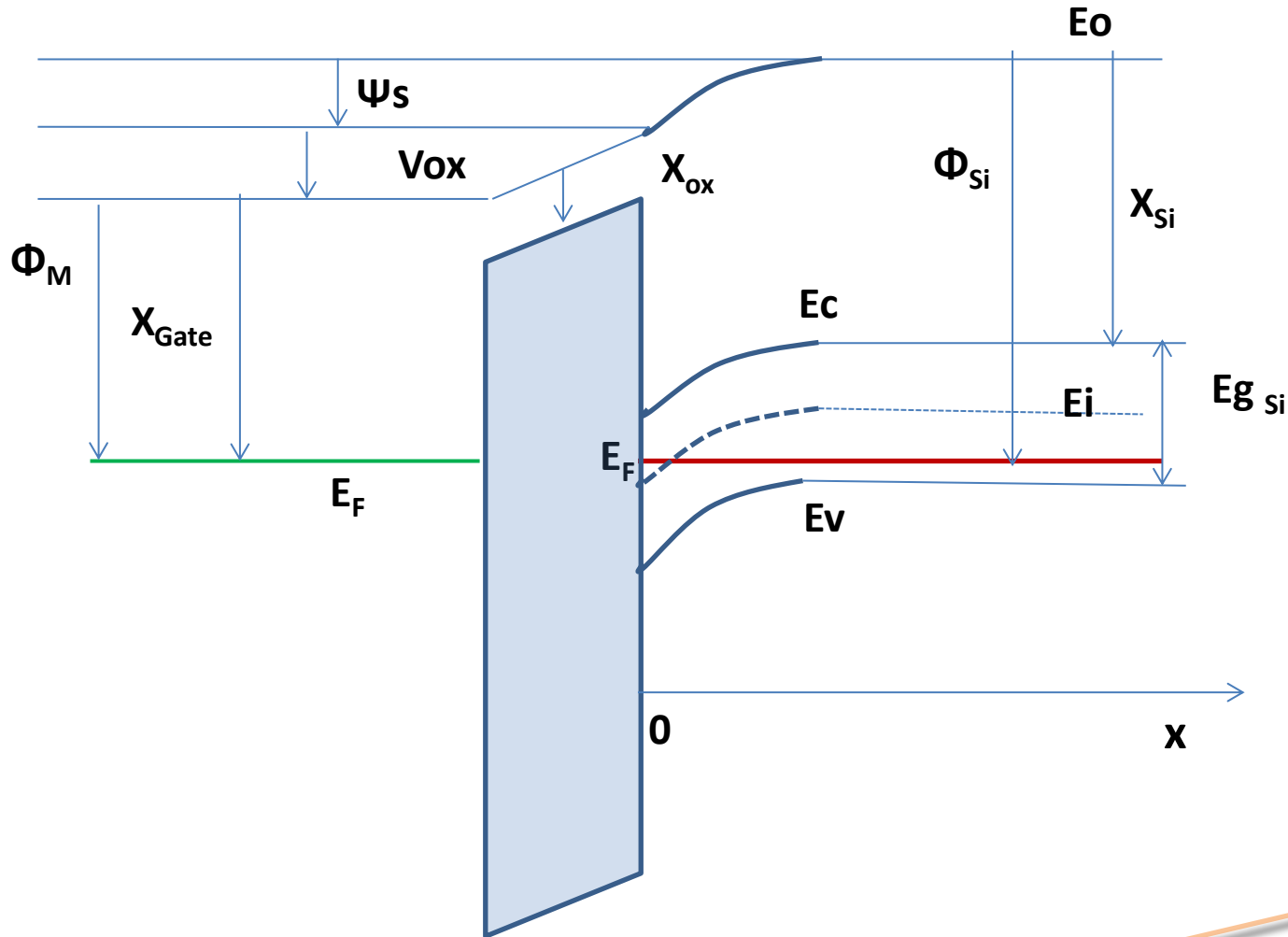


Band Diagram: Metal-Oxide-Semiconductor



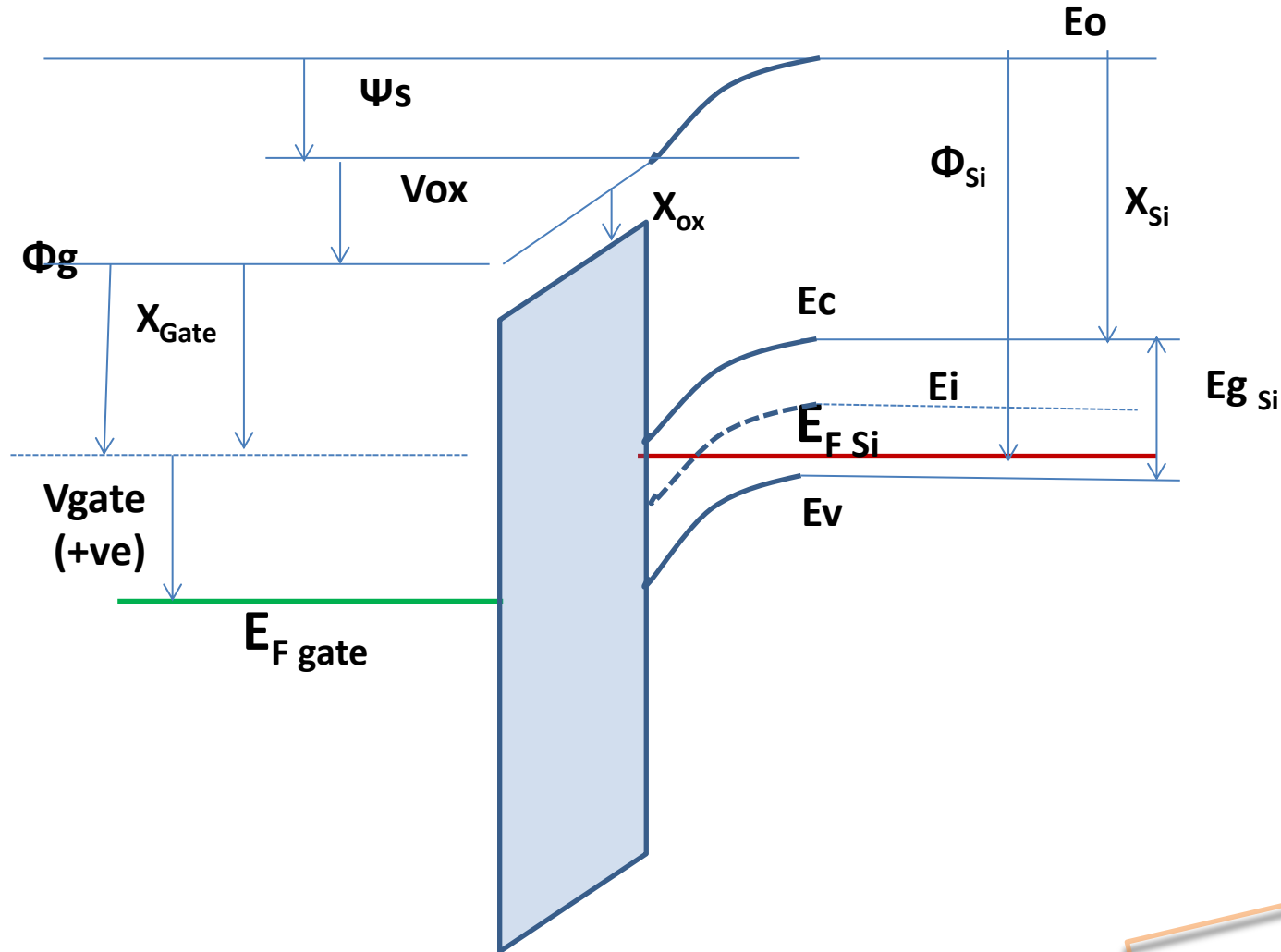


MOS Band Diagram After Contact



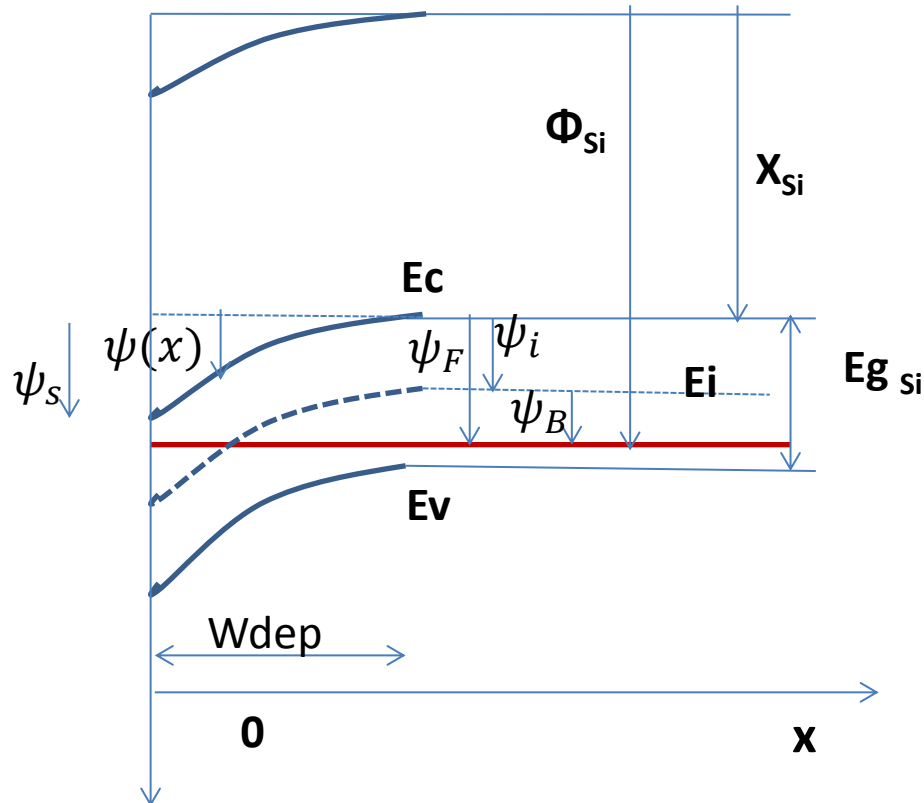


Gate Voltage Application





Charge Dependence on Potential





Poisson's Equation for N-MOS Stack

$$\frac{d^2\psi}{dx^2} = -\frac{\rho(x)}{\epsilon}$$
$$= -\frac{q}{\epsilon} [p(x) - n(x) + N_D^+(x) - N_A^-(x)]$$

At $x \rightarrow \infty$: **Charge Neutrality:** $p_0 - n_0 + N_D^+ - N_A^- = 0$

$$p(x) = n_i e^{q(\psi_F - \psi_i)/k_B T} = n_i e^{q(\psi_B - \psi)/k_B T} = N_A e^{-q\psi/k_B T}$$

$$n(x) = n_i e^{q(\psi_i - \psi_F)/k_B T} = n_i e^{q(\psi - \psi_B)/k_B T} = (n_i^2 / N_A) e^{q\psi/k_B T}$$

$$p_0 \approx N_A, \quad n_0 = n_i^2 / p_0 \approx n_i^2 / N_A$$

$$\frac{d^2\psi}{dx^2} = -\frac{q}{\epsilon} \left[N_A \left(e^{-\frac{q\psi}{k_B T}} - 1 \right) - \frac{n_i^2}{N_A} \left(e^{\frac{q\psi}{k_B T}} - 1 \right) \right]$$





NMOS Stack Charge Eqn.

Multiply both sides by $\left(\frac{d\psi}{dx}\right) dx$ (which is also $= dx$):

$$\frac{d^2\psi}{dx^2} \frac{d\psi}{dx} dx = \frac{d}{dx} \left[\frac{d\psi}{dx} \right] \frac{d\psi}{dx} dx = \frac{d\psi}{dx} d \left[\frac{d\psi}{dx} \right]$$

$$\frac{d\psi}{dx} d \left[\frac{d\psi}{dx} \right] = -\frac{q}{\epsilon} \left[N_A \left(e^{-\frac{q\psi}{k_B T}} - 1 \right) - \frac{n_i^2}{N_A} \left(e^{\frac{q\psi}{k_B T}} - 1 \right) \right] d\psi$$

Integrate both sides: LHS: from $\frac{d\psi}{dx} = \frac{d\psi_s}{dx}$ at $x = 0$ to $\frac{d\psi}{dx} = 0$ at $x = \infty$

RHS: from $\psi = \psi_s$ at $x = 0$ to $\psi = 0$ at $x = \infty$

$$\left(\frac{d\psi_s}{dx} \right)^2 = \frac{2K_B T N_A}{\epsilon_{si}} \left[\left(e^{-\frac{q\psi_s}{k_B T}} + \frac{q\psi_s}{KT} - 1 \right) + \frac{n_i^2}{N_A^2} \left(e^{\frac{q\psi_s}{k_B T}} - \frac{q\psi_s}{KT} - 1 \right) \right]$$



Surface Charge (Q_s)

$$\left(\frac{d\psi_s}{dx}\right)^2 = F_s^2$$

From Poisson's equation:

$$\int_{F_s}^0 F dF = \frac{1}{\epsilon_{si}} \int_0^{W_{dep}} \rho dx \rightarrow 0 - F_s = \frac{1}{\epsilon_{si}} Q_s$$

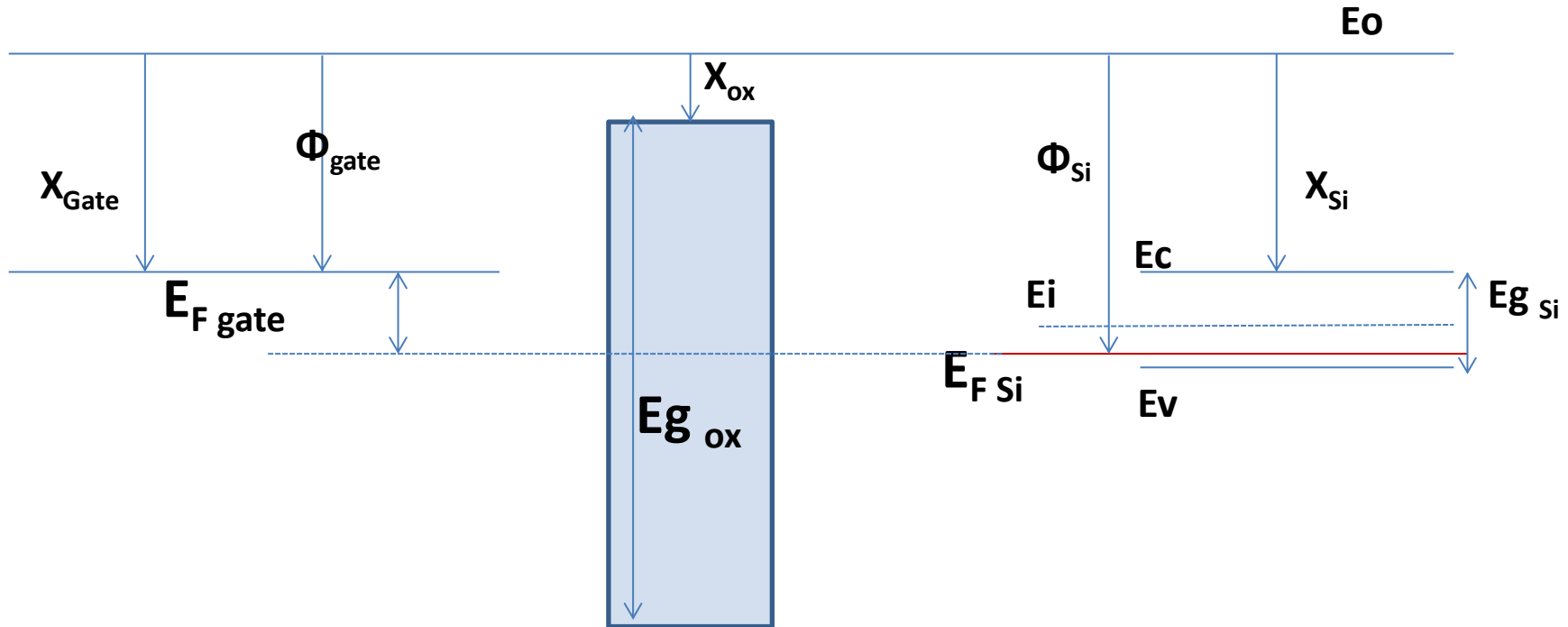
$$Q_s = -\epsilon_{si} F_s = -\epsilon_{si} \sqrt{\left(\frac{d\psi_s}{dx}\right)^2}$$

$$Q_s = \pm \sqrt{2\epsilon_{si} K_B T N_A} \left[\left(e^{-\frac{q\psi_s}{k_B T}} + \frac{q\psi_s}{KT} - 1 \right) + \frac{n_i^2}{N_A^2} \left(e^{\frac{q\psi_s}{k_B T}} - \frac{q\psi_s}{KT} - 1 \right) \right]^{1/2}$$





Flatband Voltage (V_{FB})



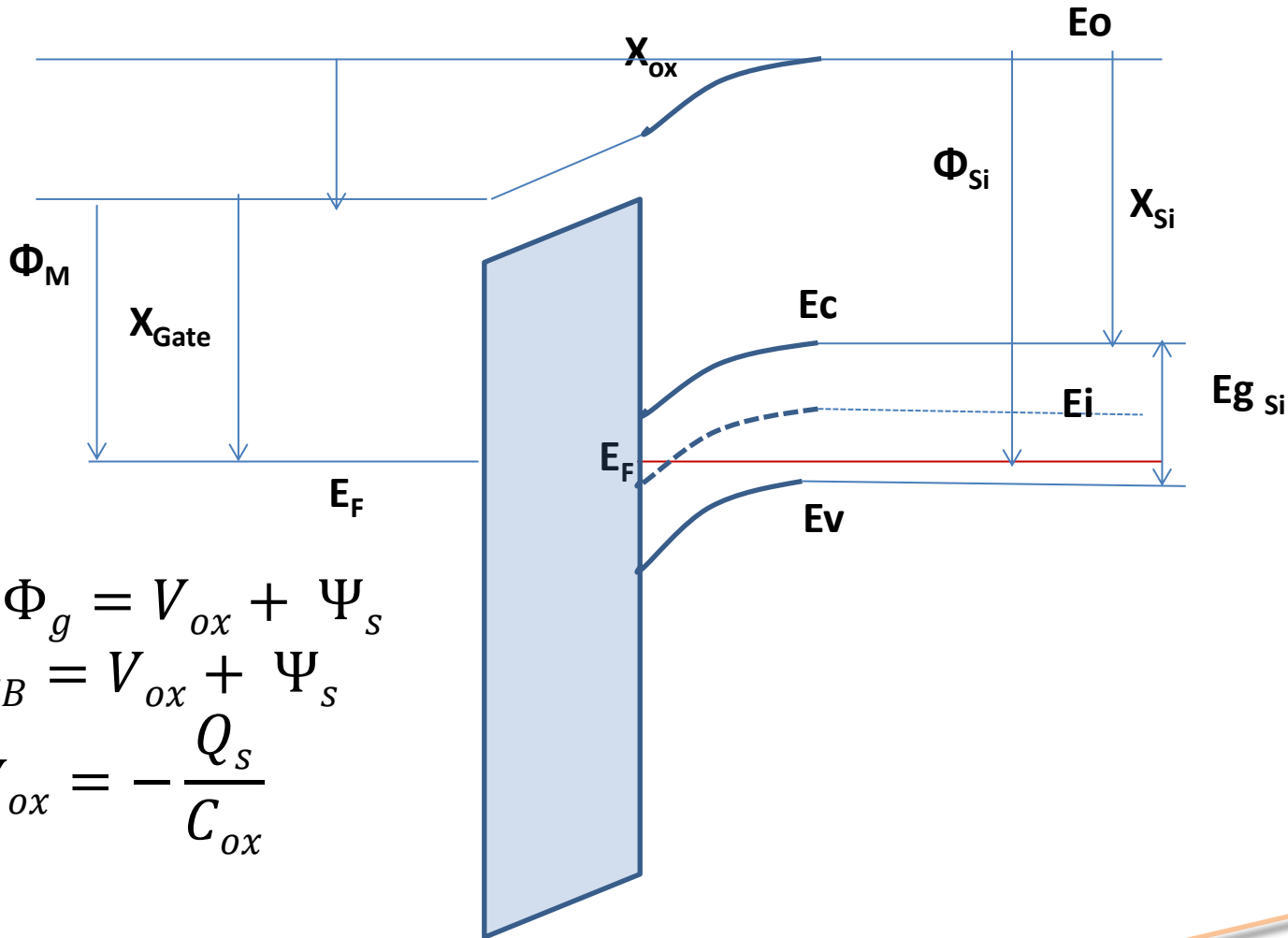
$V_{FB} = \text{Gate Workfunction} - \text{Semiconductor Workfunction}$

$$qV_{FB} = \Phi_{gate} - \Phi_{Si} = E_{F gate} - E_{F Si}$$





Potential Drop Equation: No Applied Gate Voltage



$$\Phi_{si} - \Phi_g = V_{ox} + \Psi_s$$

$$-V_{FB} = V_{ox} + \Psi_s$$

$$V_{ox} = -\frac{Q_s}{C_{ox}}$$





Potential Drop Equation: Applied Gate Voltage

$$V_g + (\Phi_{si} - \Phi_g) = V_{ox} + \Psi_s$$

$$V_g - V_{FB} = V_{ox} + \Psi_s$$

$$V_{ox} = -\frac{Q_s}{C_{ox}}$$

In Inversion:

$$Q_s = Q_{dep} + Q_{inv}$$

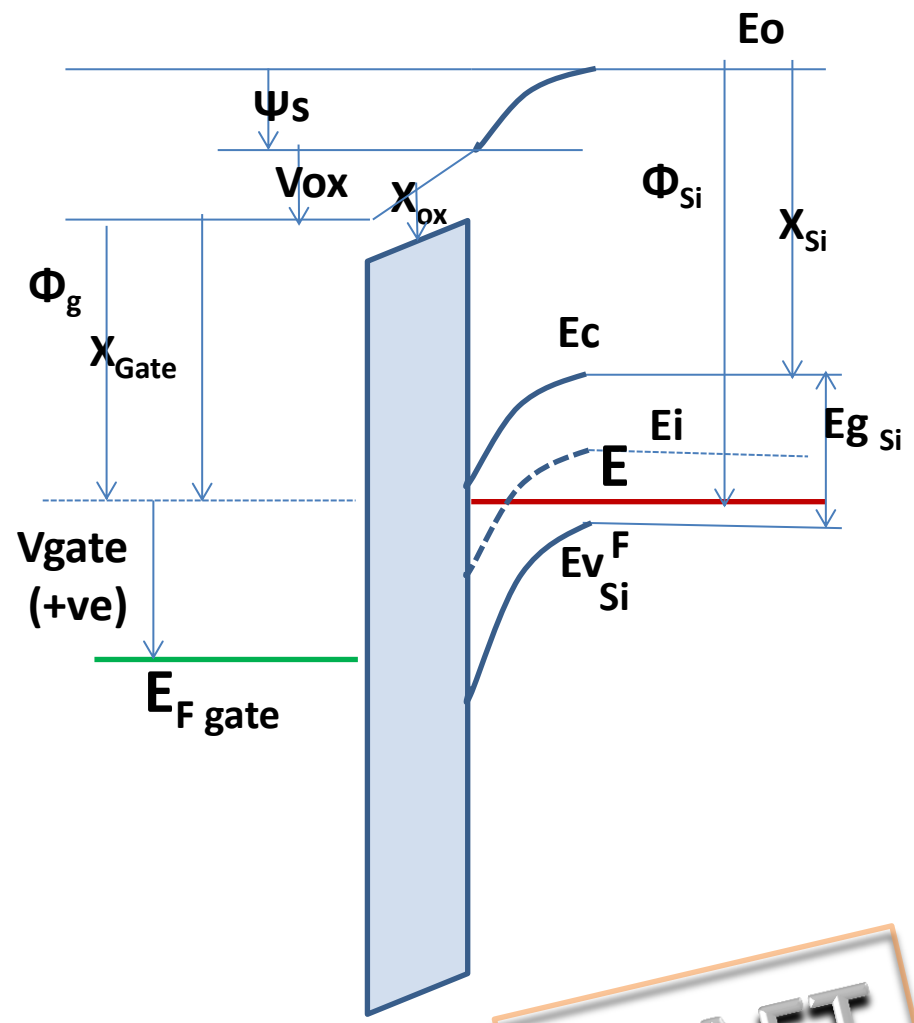
$$Q_{dep} = -qN_A W_{dep} = -\sqrt{2\epsilon_{si} q N_A \Psi_s}$$

In Strong Inversion:

$$Q_{inv} \approx -\sqrt{\frac{2\epsilon_{si} K_B T n_i^2}{N_A}} e^{\frac{q\psi_s}{2K_B T}}$$

In-between: use Q_s equation

In Depletion: $Q_s \approx Q_{dep}$



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Threshold Voltage (V_{th}) under Depletion Approximation

At $0 > \Psi_s \geq 2 \Psi_{Bulk}$:

- No free carriers (i.e. no inversion electrons)
- Only depletion charges from ionized dopants

At $\Psi_s \geq 2 \Psi_{Bulk}$:

- No more changes in surface potential
- Fixed Q_{dep}
- Only changes in inversion electrons
- V_{gate} at $\Psi_s \geq 2 \Psi_{Bulk}$ is called Threshold Voltage (V_{th})

Using: $V_{gate} = V_{FB} - \frac{Q_s}{C_{ox}} + \Psi_s$

At “Onset” of Strong Inversion: $V_{th} = V_{FB} - \frac{Q_{dep}}{C_{ox}} + 2\Psi_{Bulk}$

$$= V_{FB} + \frac{\sqrt{2\varepsilon_{si}qN_A(2\Psi_{Bulk})}}{C_{ox}} + 2\Psi_{Bulk}$$



Inversion Charge (V_{th}) under Depletion Approximation

In Strong Inversion ($V_g > V_{th}$):

$$V_{gate} = V_{FB} - \frac{Q_{dep} + Q_{inv}}{C_{ox}} + 2\Psi_{Bulk} = V_{FB} - \frac{Q_{dep}}{C_{ox}} + 2\Psi_{Bulk} - \frac{Q_{inv}}{C_{ox}}$$

$$V_{gate} = V_{th} - \frac{Q_{inv}}{C_{ox}}$$

$$\rightarrow Q_{inv} = -C_{ox}(V_{gate} - V_{th})$$



Capacitance-Voltage (C-V) Characteristics

$$\text{Small Signal: } C_C(V_g) = dQ_C/dV_C$$

