



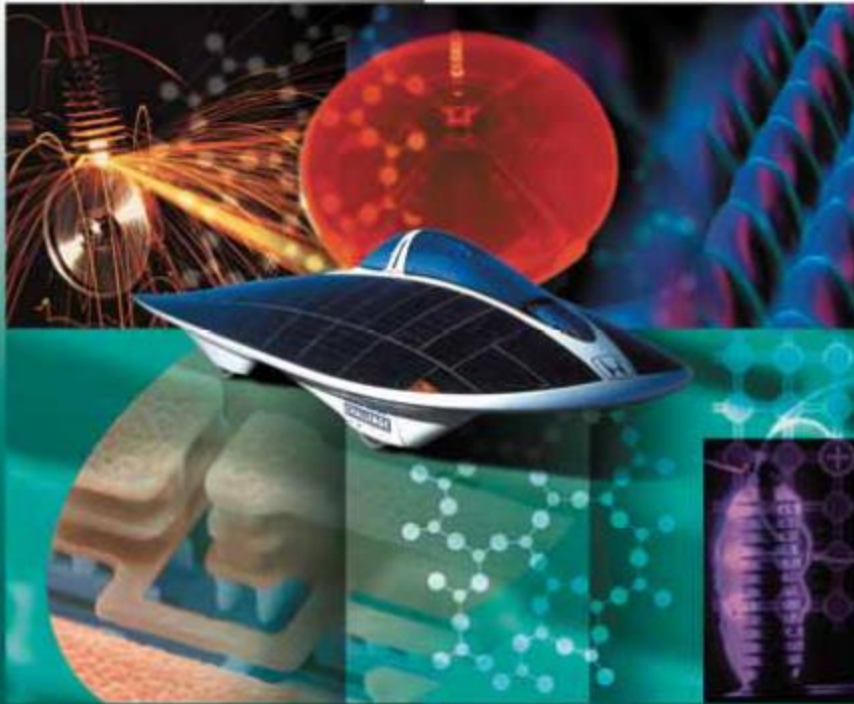
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# Lec. 7: Hydrogen Potential

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# Principles of Electronic Materials and Devices

Third Edition



S. O. Kasap

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# Pages



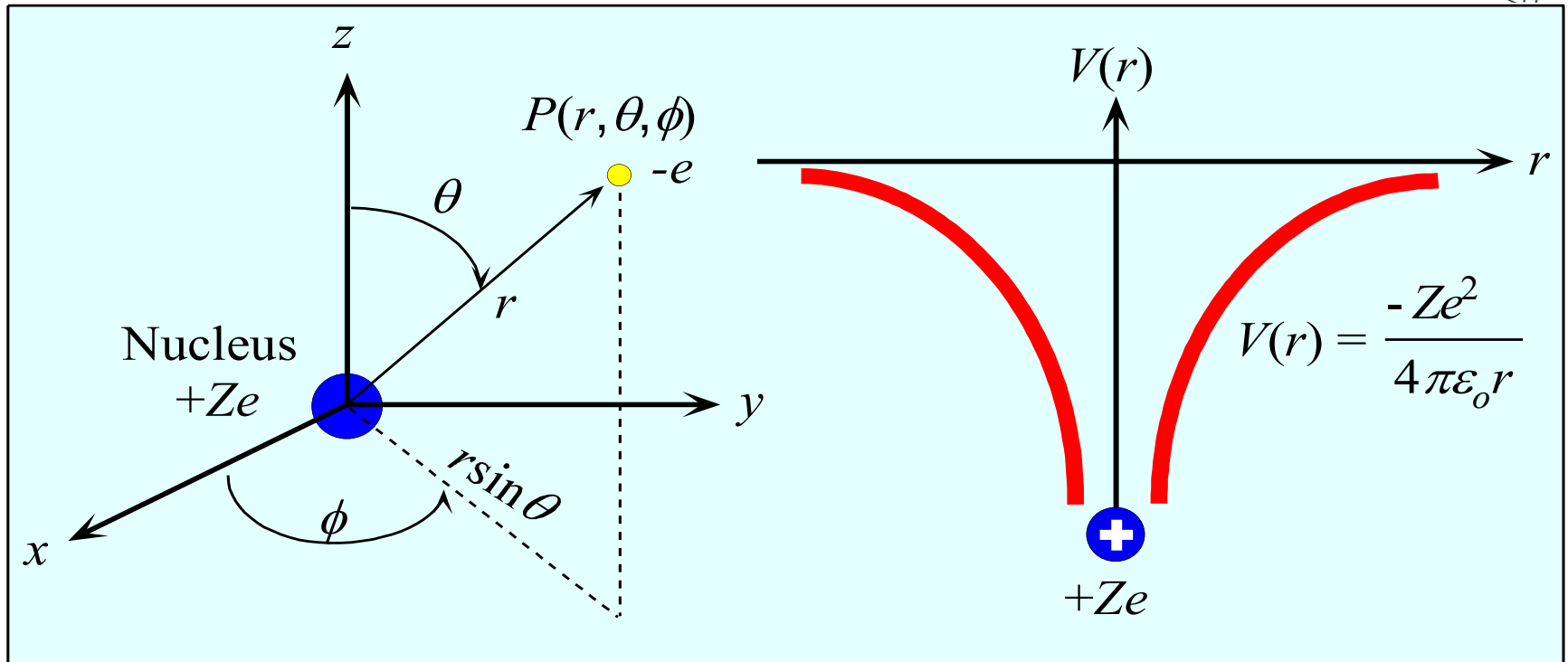
P. 231-234: Hydrogen Atom

# Outline



- Energy Levels in Hydrogen
- Overlap of Hydrogen Atom potential and wavefunction
- Band Theory using Hydrogen

# Hydrogen Potential Well



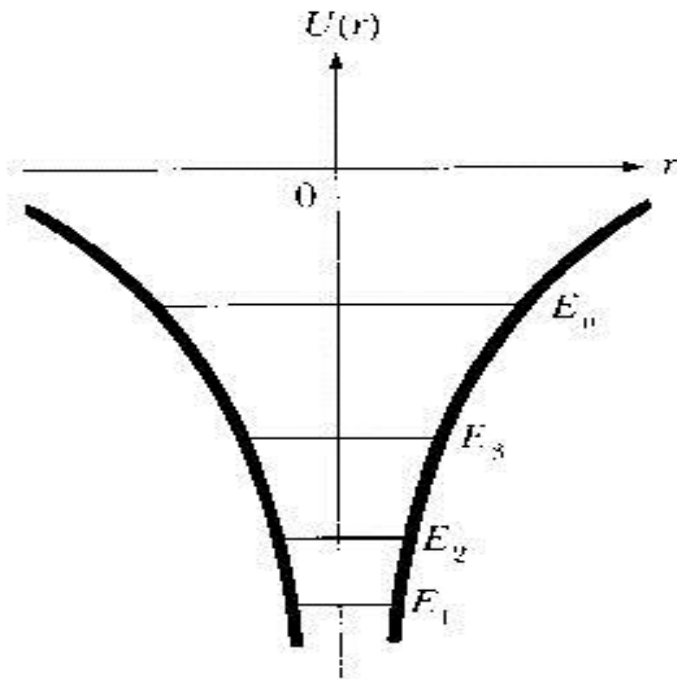
The electron in the hydrogenic atom is attracted by a central force that is always directed towards the positive nucleus. We therefore use spherical coordinates centered at the nucleus to describe the position of the electron. The  $PE$  of the electron depends on  $r$  only.



# Discrete Energy Levels

This is a “Potential Well” where Schrodinger equation has solution inside it (like in 1-D box) and outside it (like in barrier tunneling)

i.e. It has discrete energy levels and finite wavefunctions



$$U(r) = -\frac{1}{4\pi\epsilon_0} \frac{e^2}{r}$$

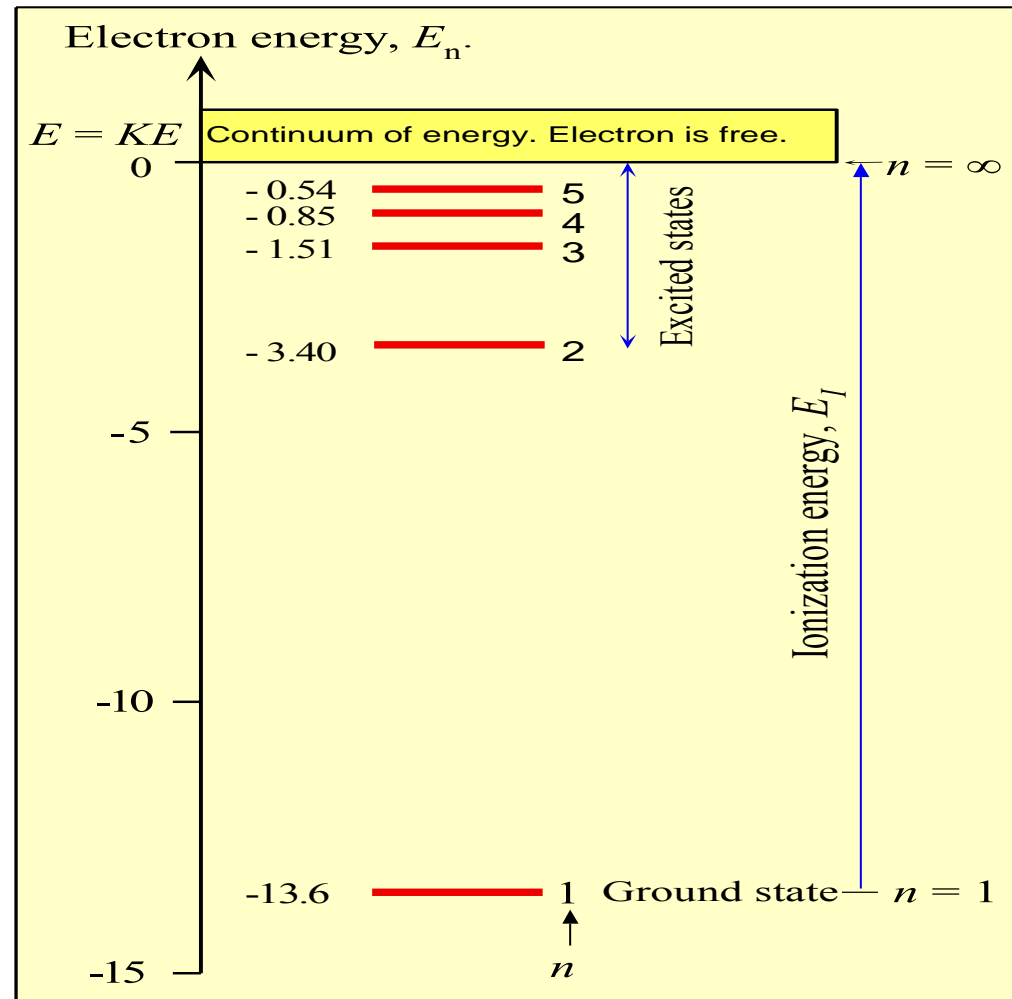
# Energy Levels for H-atom:

Depends on *Principal Quantum Number*



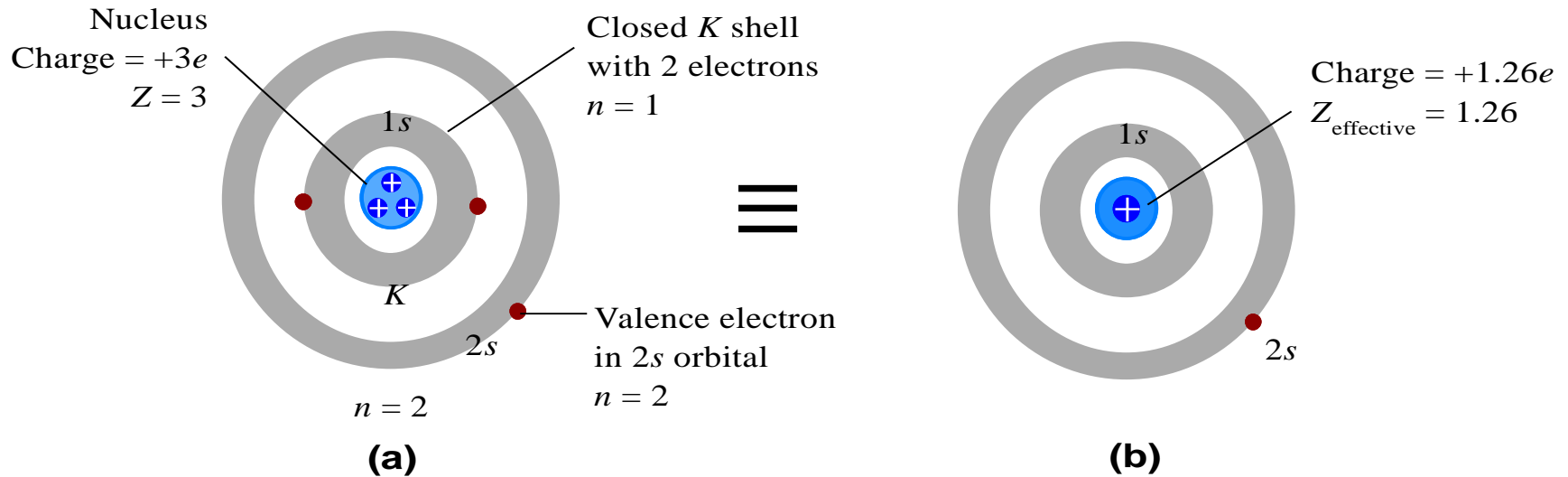
$$E_n = -\frac{Z E_1}{n^2}$$

$$E_1 = \frac{me^4}{8\epsilon_0 h^2}$$



The energy of the electron in the hydrogen atom ( $Z = 1$ )

# $Z_{\text{Effective}}$ : (1.26 for Li)

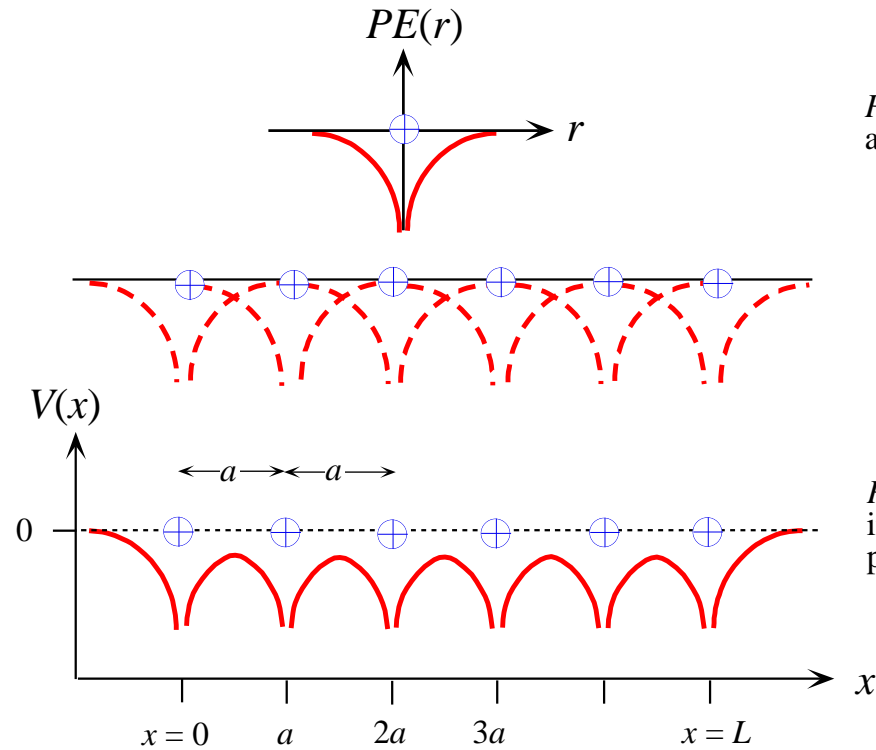


The Li atom has a nucleus with charge  $+3e$ , 2 electrons in the K shell, which is closed, and one electron in the 2s orbital.

(b) A simple view of (a) would be one electron in the 2s orbital that sees a single positive charge,  $Z=1$



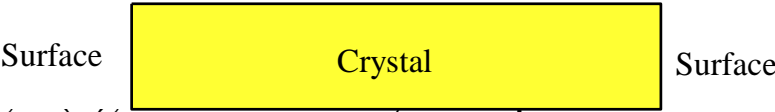
# Superposition of Coulomb Potential for N-Atoms



$PE$  of the electron around an isolated atom

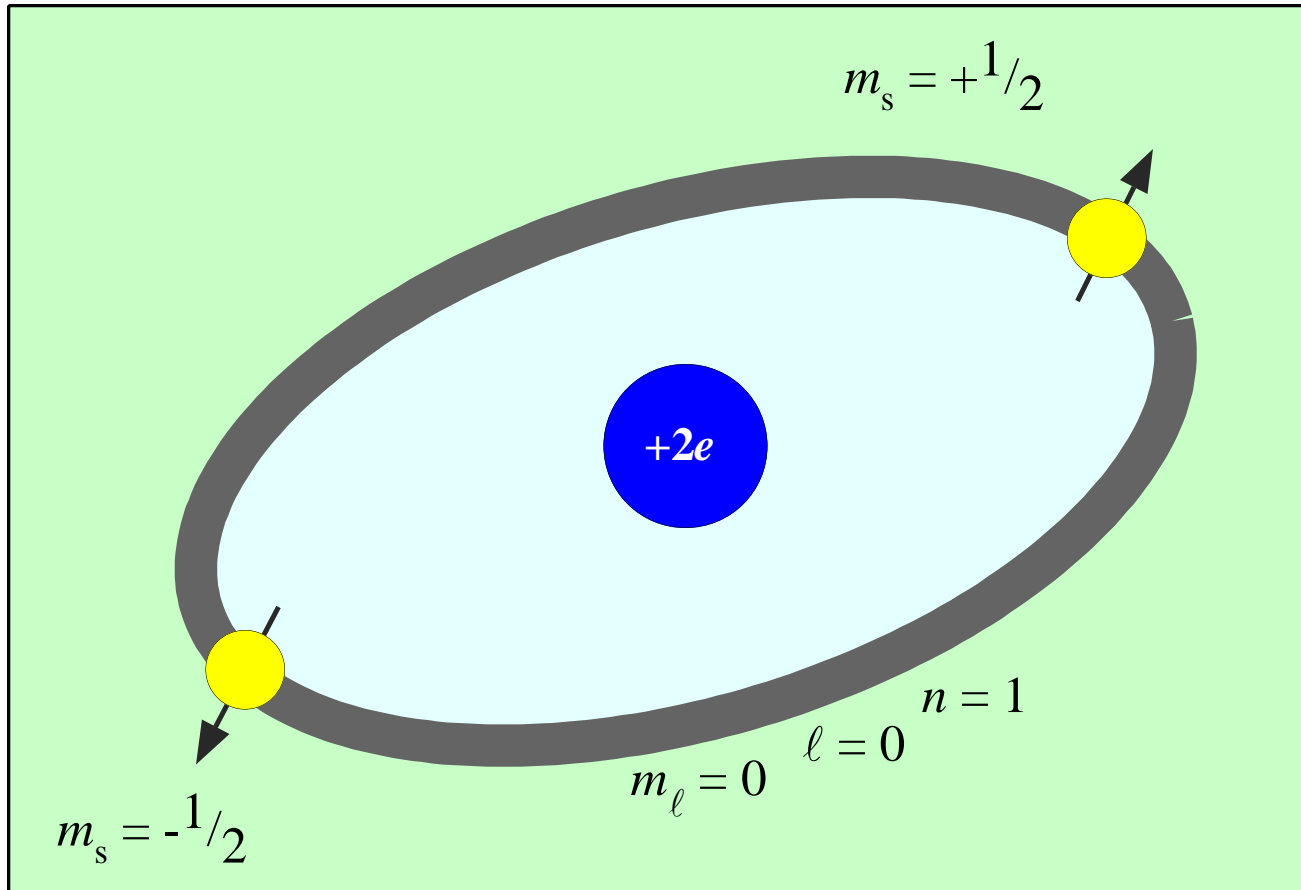
When  $N$  atoms are arranged to form the crystal then there is an overlap of individual electron  $PE$  functions.

$PE$  of the electron,  $V(x)$ , inside the crystal is periodic with a period  $a$ .

The electron  $P$   periodicity as that of the crystal,  $a$ . Far away outside the crystal, by choice,  $V = 0$  (the electron is free and  $PE = 0$ ).



# Paired Spins



Paired spins in an orbital.



# Pauli's Exclusion Principle:

*No two electrons can have the same four quantum numbers within the same system*

**Table 3.3** The four quantum numbers for the hydrogenic atom

$n$	Principal quantum number	$n = 1, 2, 3, \dots$	Quantizes the electron energy
$\ell$	Orbital angular momentum quantum number	$\ell = 0, 1, 2, \dots (n - 1)$	Quantizes the magnitude of orbital angular momentum $L$
$m_\ell$	Magnetic quantum number	$m_\ell = 0, \pm 1, \pm 2, \dots, \pm \ell$	Quantizes the orbital angular momentum component along a magnetic field $B_z$
$m_s$	Spin magnetic quantum number	$m_s = \pm \frac{1}{2}$	Quantizes the spin angular momentum component along a magnetic field $B_z$