



# EC630 - Modern Electronics Circuits

## Noise Modeling

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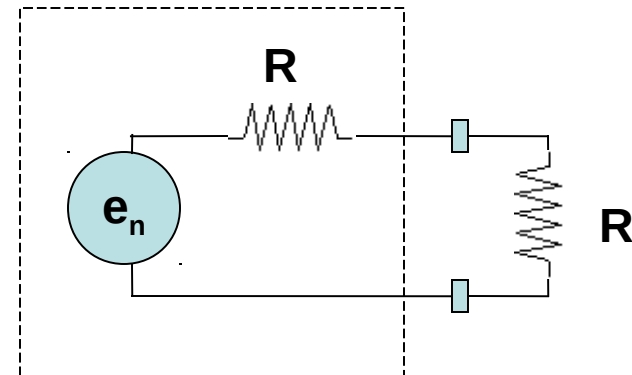


# Outline

- Thermal Noise Types in Resistors
- Thermal Noise Types in MOSFETs



# Thermal Noise of a Resistor “R”



- Available noise power,  $P_{NA}$ :

$$P_{NA} = kT \Delta f$$

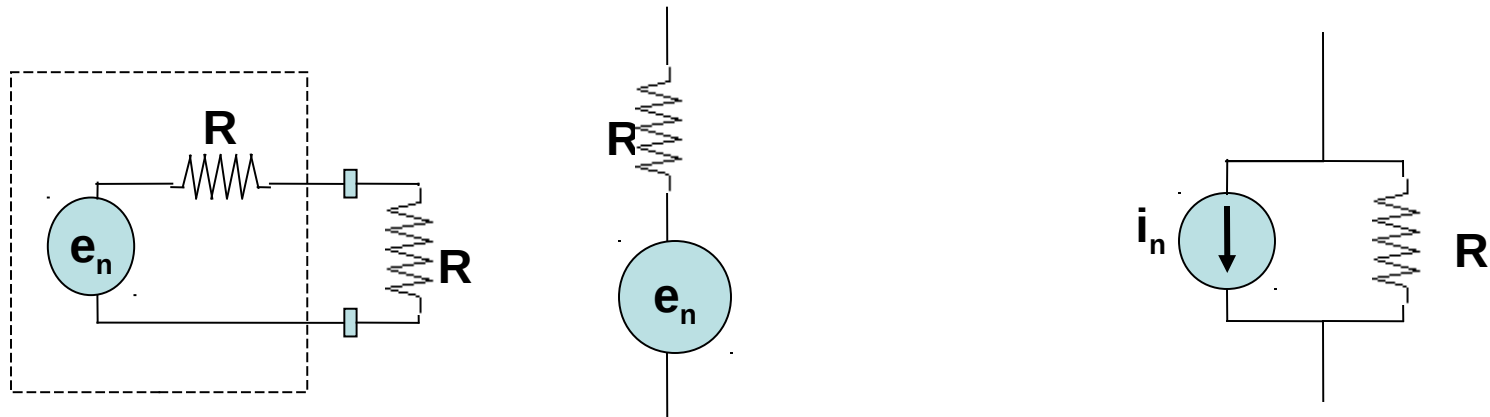
$P_{NA}$  = Max. power generated by noise source which can be delivered to load, i.e. to a load of same value “R”

$\Delta f$  = Equivalent sharp filter cutoff frequency (usually higher than regular 3dB point, become close at higher order filters)

$T$  = Absolute Temp.,  $k$  = Boltzmann’s Constant



# Thermal Noise of a Resistor “R”



- Max. power is delivered when load = R:

$$P_{NA} = kT \Delta f = e_n^2 / 4R$$

$$e_n^2 = 4kT R \Delta f$$

$$i_n^2 = e_n^2 / R^2 = 4kT \Delta f / R$$



# Sources of Thermal Noise

- Random motion due to thermal energy translates to potential fluctuations



# MOSFET Noise: Drain Current Noise

- MOSFET channel, specially in triode region, is a voltage controlled resistance
- Drain current noise current,  $i_{nd}$ :

$$i_{nd}^2 = 4kT \gamma g_{do} \Delta f$$

$g_{do}$  = drain-source conductance as  $V_{ds}$  tends to zero

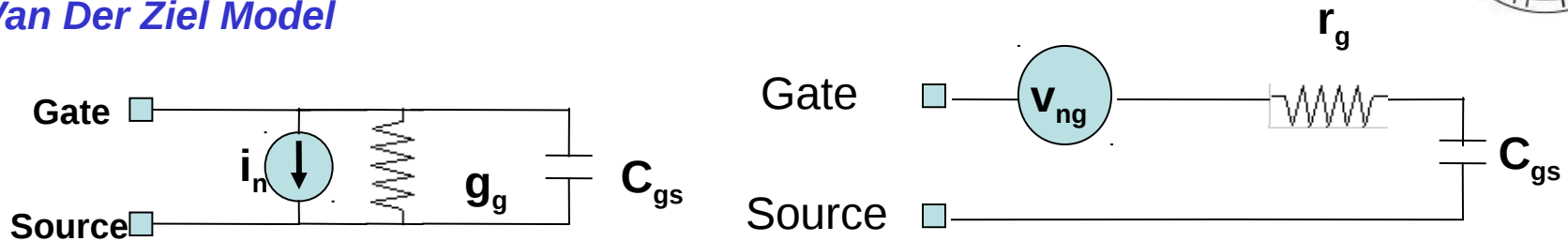
$\gamma$  = a parameter that starts at 1 at  $V_{ds}=0$ , then tends to 2/3 in saturation, for long channel devices

- Typically only for NMOS within normal operation range



# MOSFET Noise: Gate Noise

## Van Der Ziel Model



- Thermal agitation of electrons in channel cause potential fluctuation, which in turns couples capacitively to gate
- Gate noise current,  $i_{ng}$ :

$$i_{ng}^2 = 4kT \delta g_g \Delta f$$

$g_g = \omega^2 C_{gs}^2 / 5g_{do}$  = equivalent shunt gate-to-source conductance

$\delta$  = a parameter that tends to 4/3 for long channel devices

$$r_g = 1/[g_g (Q^2+1)] \sim 1/ (g_g Q^2) = 1/ 5g_{do}$$

$$v_{ng}^2 = 4kT \delta r_g \Delta f$$